

# Preserving Link Privacy in Social Network Based Systems

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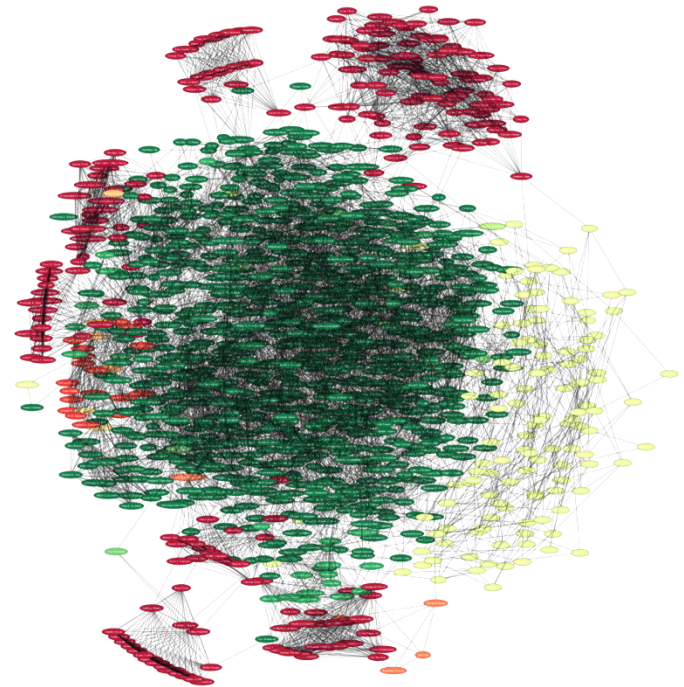
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# Social Networks

- Social links indicate shared interests and trust
- Social graph data is a key enabler



- Recommendation systems
- Reputation systems
- Sybil defenses
- Anonymous communications
- Censorship resistance

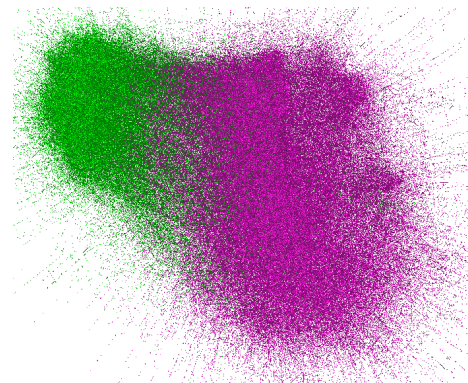
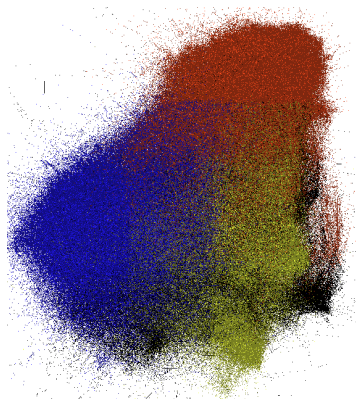


# Lack of Privacy of Social Contacts

- Social contacts are private information
  - 52% Facebook users hide social contacts [NYU 2011]
- Problem: social contacts are **revealed** to adversaries in existing applications.

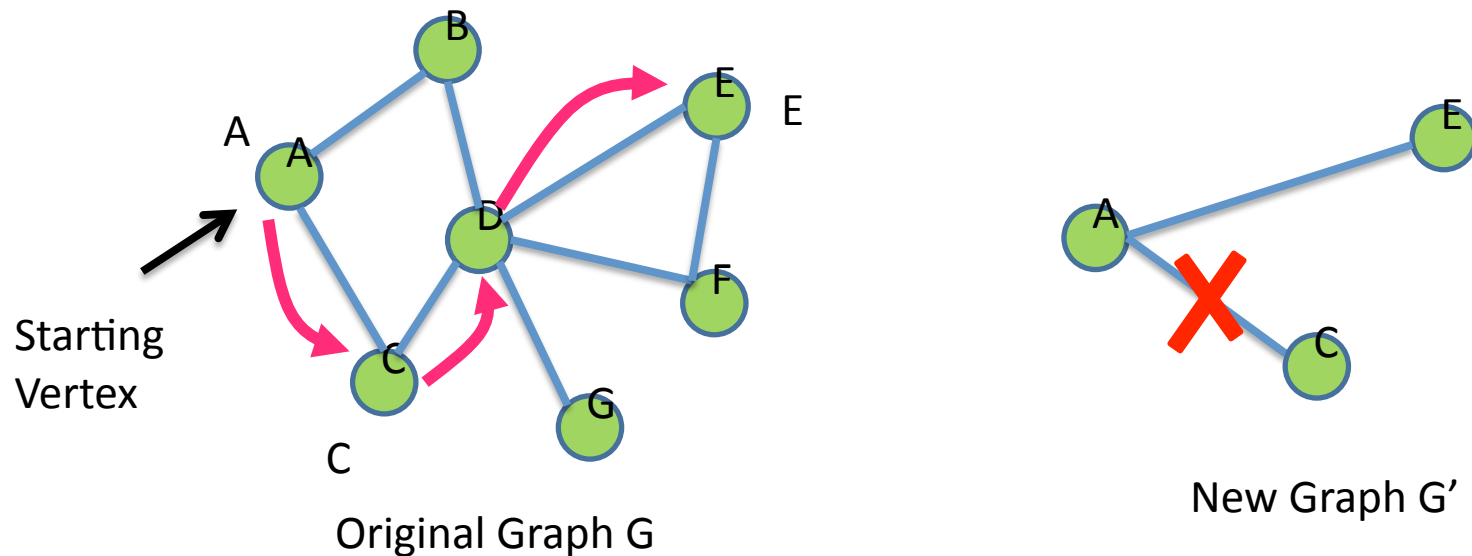
# How to Balance Application Utility vs Link Privacy?

- Idea: OSN operator can add **noise** to the social graph
  - Delete real links
  - Add fake links
- Challenge: Need to preserve **community structures** in social networks



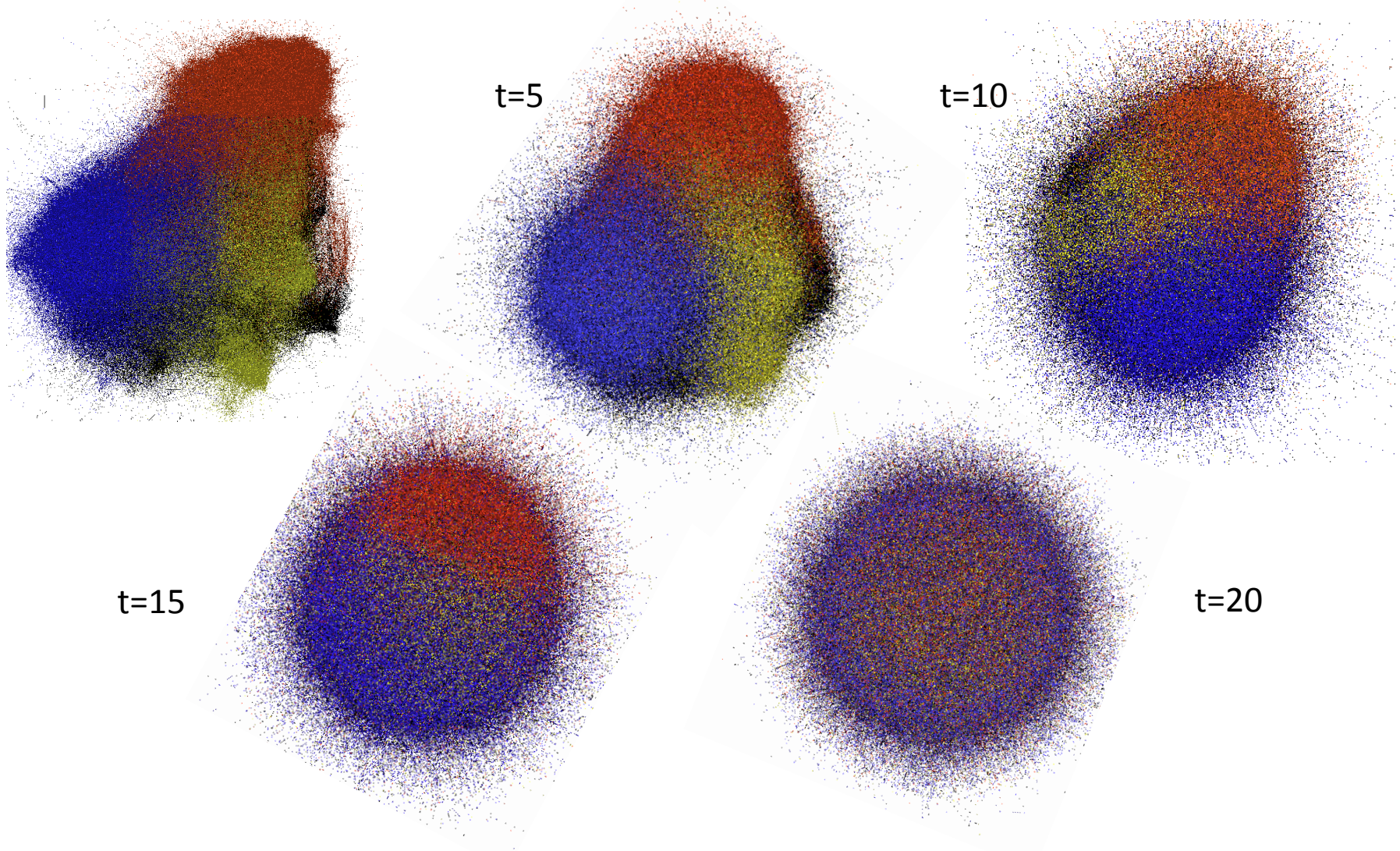
# Structured Graph Perturbation

- Capture structural properties via random walks

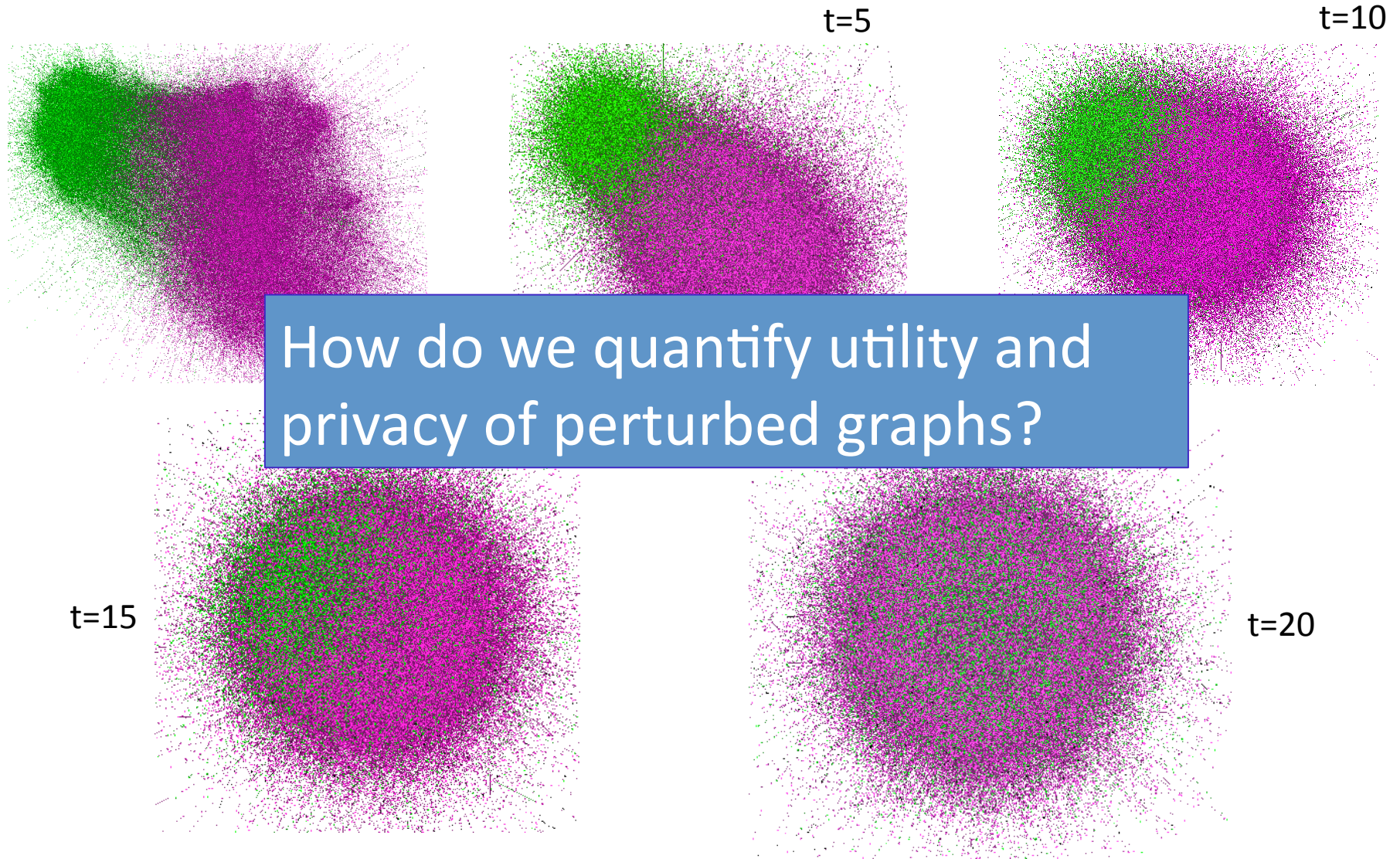


$t \rightarrow$  random walk length. Trade off between privacy and utility

# Facebook Friendship Subgraph: 63,392 users and 816,886 edges



# Facebook Interaction Subgraph: 43,953 users and 182,384 edges



# Key Results

- Characterizing Privacy
  - Bayesian approach
  - Risk based approach
- Characterizing Utility
  - Perspective of vertex
  - Change in vertex neighborhood
- Applications
  - Secure routing, Sybil defenses



# Characterizing Privacy: Bayesian Approach

- Bayesian Formulation

- $G \rightarrow$  original graph

- $G' \rightarrow$  perturbed graph

- $H \rightarrow$  prior information

} Adversary has  $G'$  and  $H$

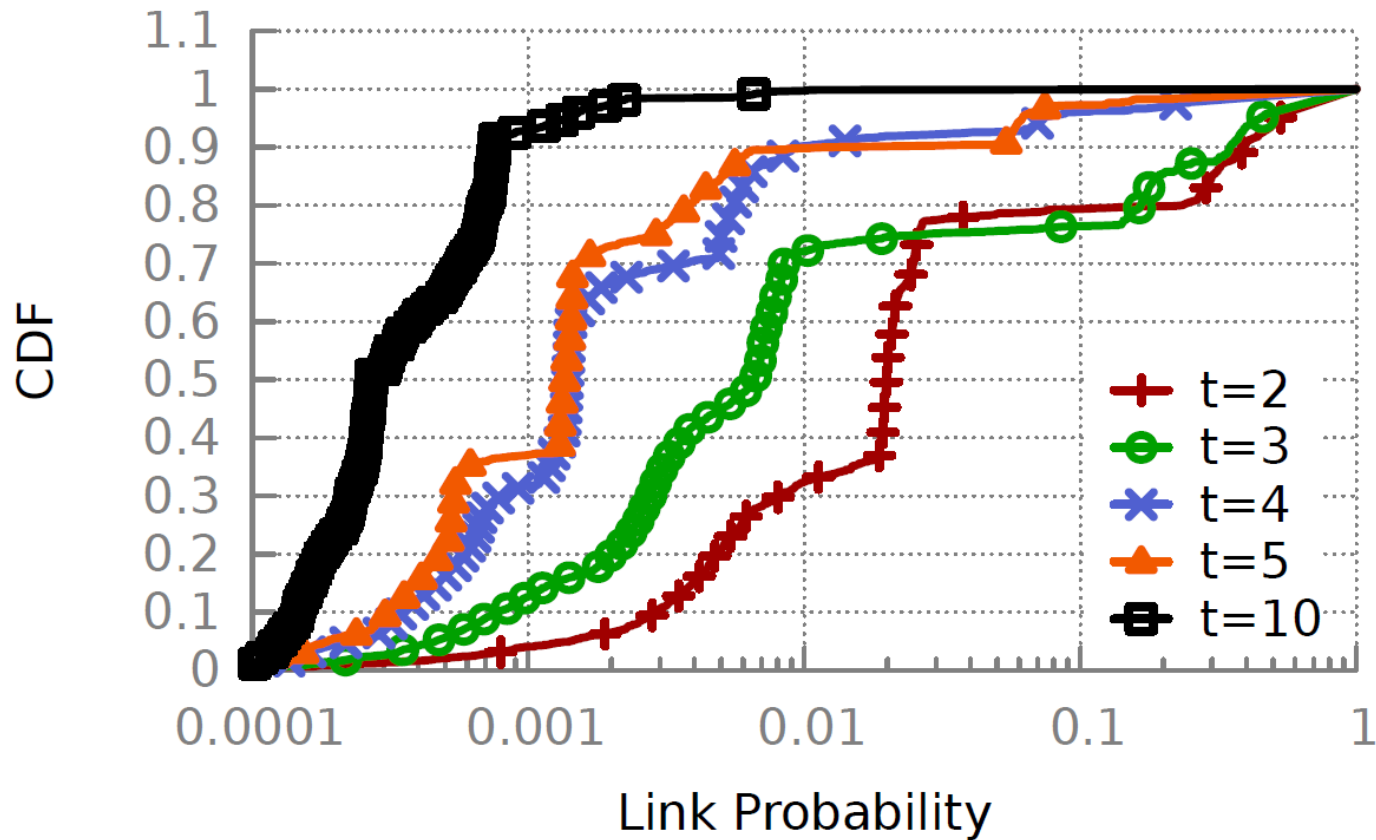
- What is the privacy of a link  $L$ ?

- $P(L \in G \mid G', H)$

- $P(L \in G \mid G', H) = \frac{P(G' \mid L, H) \cdot P(L \mid H)}{P(G' \mid H)}$

Probability of producing  $G'$  given  $L$  and prior  $H$

# Bayesian Privacy Analysis: Interaction Graph



# Applications: Secure Routing

## Sprout DHT (Chord + Social Links)

**Table 1. Path reliability using Sprout for a linear trust decay model.**

Facebook interaction graph		Facebook friendship graph	
Mechanism	Reliability	Mechanism	Reliability
Original	0.110	Original	0.140
$t = 3$	0.101	$t = 3$	0.126
$t = 5$	0.101	$t = 5$	0.121
$t = 10$	0.096	$t = 10$	0.118
Chord	0.075	Chord	0.072

# Summary

- **Structured Graph Perturbation**
  - Preserves link privacy
  - Preserves community structures
- Metrics for utility and privacy
- Applications
  - Community structure based