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# Does Counting Still Count?

Revisiting the Security of Counting based User Authentication Protocols against Statistical Attacks

Hassan Jameel Asghar<sup>1</sup>, Shujun Li<sup>2</sup>

Ron Steinfeld<sup>3</sup>, Josef Pieprzyk<sup>1</sup>

<sup>1</sup>Macquarie University, Australia

<sup>2</sup>University of Surrey, UK

<sup>3</sup>Monash University, Australia

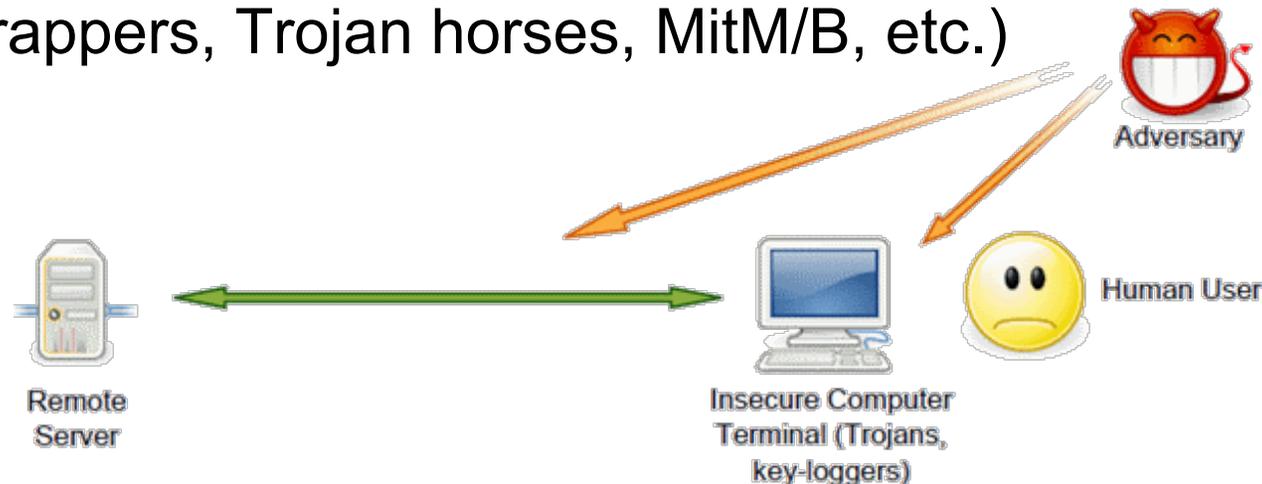
[hassan.asghar@mq.edu.au](mailto:hassan.asghar@mq.edu.au), [shujun.li@surrey.ac.uk](mailto:shujun.li@surrey.ac.uk)

[ron.steinfeld@monash.edu](mailto:ron.steinfeld@monash.edu), [josef.pieprzyk@mq.edu.au](mailto:josef.pieprzyk@mq.edu.au)

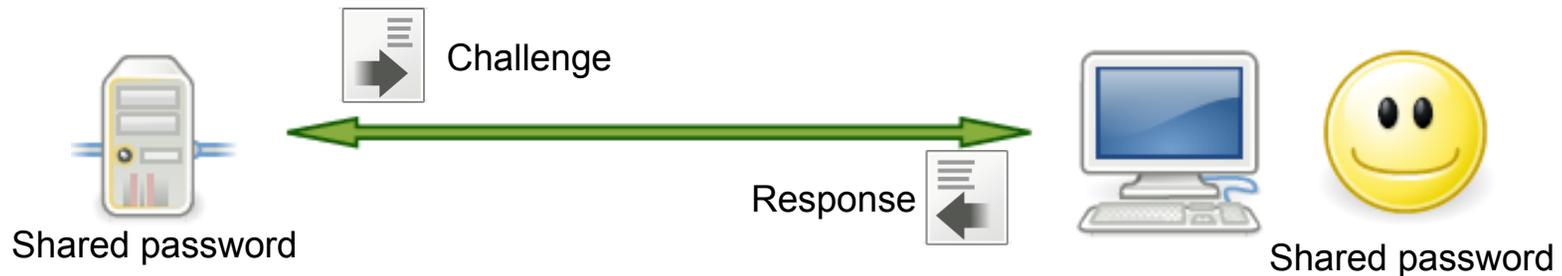
**Surrogate Presenter: Ehab El-Shaer (UNCC)**

- An Old Problem: Unassisted Human Authentication against Observers (1990s-)
- A New Threat: Yan et al.'s 2D Statistical Attack (NDSS 2012)
- Our Contributions
  - Why does Yan et al.'s attack work? – A general theoretical analysis of  $\delta D$  statistical attacks ( $\delta \geq 1$ ) on counting based protocols
  - An approach for estimating the security bound
  - New principles and fixes to make counting based protocols more secure against the new attacks

- How to authenticate an **unassisted** human user on an **observable** (**untrusted**) terminal?
  - Why **unassisted**? – Hardware devices cause usability problems and may be attacked as well.
  - Who are **observers**? – Shoulder surfers, hidden cameras, card skimmers, malware (keyloggers, screen scrappers, Trojan horses, MitM/B, etc.)



- Challenge-response protocols proposed as general solutions to hide the shared secret  $P$  in challenges  $C=f_C(P)$  and responses  $R=f_R(P,C)$ .



- Many solutions exist, but the main research question remains **unanswered**:
  - How to make a protocol which is both usable and secure against adversary with **many** observed sessions?

# Solutions based on counting?

- Many proposed solutions follow this approach.
- Password  $P = k$  pass-objects out of  $n$  objects
- Challenge  $C = l$  objects ( $l \leq n$ )
- Response  $R$ 
  - Count pass-objects  $P$  in  $C \Rightarrow \#C(P)$
  - Response  $R = f_R(\#C(P))$ , e.g.  $R = \#C(P) \bmod 2$
- Why counting?
  - Recognizing objects and counting are believed easy tasks for most human users!



## Foxtail:

### A typical counting based protocol

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- Proposed by Li & Shum in 2001/2002 (published as an IACR ePrint in 2005)
- Claimed to be secure: given  $O(n)$  observed sessions, the adversary's chance of success is  $2^{-n}$ .
- Usability is better than other solutions with similar security, but still not practical (2-3 minutes).
- At NDSS 2012 Yan et al. reported a statistical attack which can fully recover  $P$  with  $O(n)$  observed sessions.
  - The attack can be generalized to other counting based protocols.

# How does Foxtail work?

- Challenge  $C$  of size  $2l = C_1 + C_2$  (each of size  $l$ )
  - Uni-Rule:  $C_1$  is generated such that there are 0, 1, 2 or 3 pass-objects with equal probability.
  - Rand-Rule:  $C_2$  is generated at random (the number of pass-objects can be anything from 0 to  $\min(k, l)$ ).
- Response  $R$ 
  - $R=0$  if  $\#C(P) \bmod 4 = 0$  or  $1$ , otherwise  $R=1$
- Example



- For the above challenge  $C$ , the response  $R=0$ .

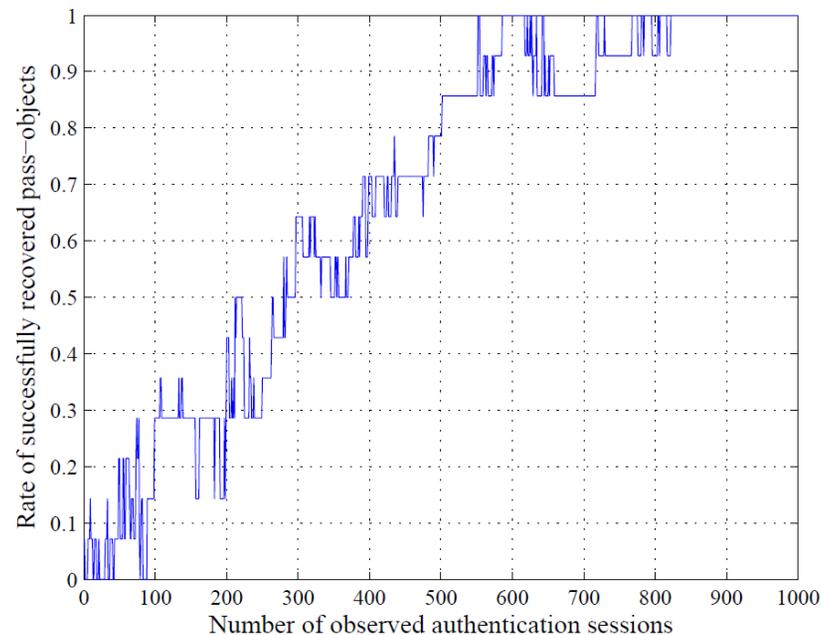
# How does Yan et al.'s attack work?

- Based on counting as well (but in 2D space)!
  - For Response 0 and 1, count the occurrences of each **object pair** ( $o_1, o_2$ ) in each challenge to get  $F_1$  and  $F_2$ .
  - Rank all objects pairs according to  $F_1 - F_2$ .
  - Take the top  $k$  distinct objects as the password.
- Why does it work?
  - No theoretical explanation, but Yan et al.'s experiments revealed pass-object pairs tend to produce larger  $F_1 - F_2$ .

Object Pairs	0-response	1-response	Difference
(1, 2)	28	24	+4
(1, 3)	32	26	+6
:	:	:	:
( $n-1, n$ )	40	28	+12

# How well does Yan et al.'s attack work to break Foxtail?

- Parameters of Foxtail:  $(n,k,l)=(140,14,15)$
- Results
  - Password recovered in about 711 authentication sessions using 2D frequency tables
  - 90% of pass-objects recovered in about 540 sessions



# Our contributions

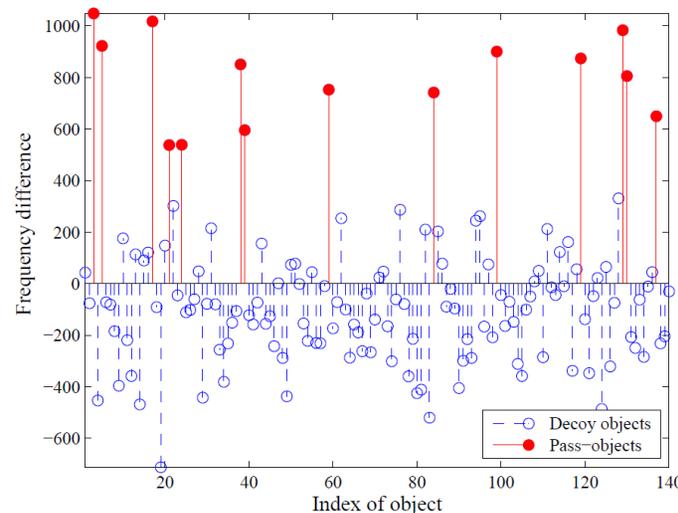
- Why does Yan et al.'s attack work?
  - Yan et al.'s 2D attack  $\Rightarrow$   $\delta$ D attack ( $\delta \geq 1$ )
  - 1D attack works as well!  $\Rightarrow$  Yan et al.'s 2D attack is just a generalization of the 1D attack to 2D space!
  - A general theoretical analysis of  $\delta$ D attack
- A theoretical approach for estimating the security lower bound against  $\delta$ D attack
  - This presentation will not cover this part due to time limit.
- Two new principles of designing new protocols
- Fixes to make counting based protocols more secure against  $\delta$ D attack (so to make counting still work)

# Why does Yan et al.'s attack work?

- Three equalities about each object's occurrence frequency must hold to disable  $\delta D$  attack
  - $\xi_{\text{pass}}(0) = \xi_{\text{decoy}}(0)$
  - $\xi_{\text{pass}}(1) = \xi_{\text{decoy}}(1)$
  - $\xi_{\text{pass}}(0) - \xi_{\text{pass}}(1) = \xi_{\text{decoy}}(0) - \xi_{\text{decoy}}(1)$
- $3\delta_{\max}$  equalities, but only 3 parameters  $(n, k, l)$
- Yan et al.'s attack works because **none** of the above equalities holds when  $\delta=2$ !
- $\Rightarrow$  Both theoretical and experimental analysis revealed that Foxtail can **never** be made theoretically secure against  $\delta D$  attack!

# 1D attack works as well!

- 1D attack also works!
  - For the default parameter  $(n,k,l)=(140,14,15)$ , the password was recovered after about 7,000 authentication sessions were observed.
  - Less efficient than 2D attack, but still a theoretical threat!
- Further analysis shows when  $\delta > 2$ , the attack still works but the number of required sessions increases drastically.



- The  $\delta D$  attacks discussed so far treat challenges corresponding to different response values separately.
- We can also treat all challenges equally without considering the response values.
- $\Rightarrow$  Two classes of statistical attacks
  - $\delta D$  RDFA = Response dependent frequency analysis
  - $\delta D$  RIFA = Response independent frequency analysis
- Foxtail was designed with only 1D RIFA in mind.
- Both attacks can be applied to many other protocols (not only counting based).

# Two new principles for designing protocols based on counting

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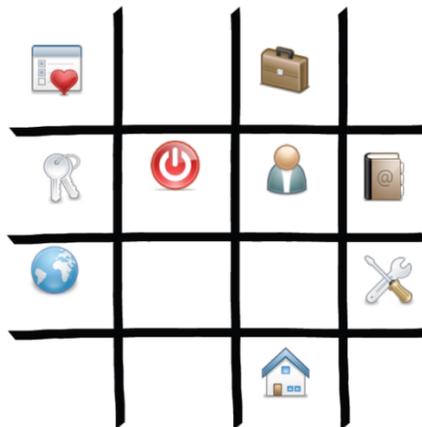
1. Each **object** should be sampled **independently** with the same probability regardless of its type (pass- or decoy objects).
  - This is to prevent RIFA.
2. The **response** should be **independent** of the number of pass-objects in each challenge.
  - This is to prevent RDFA.
  - It seems contradictory, but we will see how it may not be so.

# A general fix to any counting based protocols with binary responses

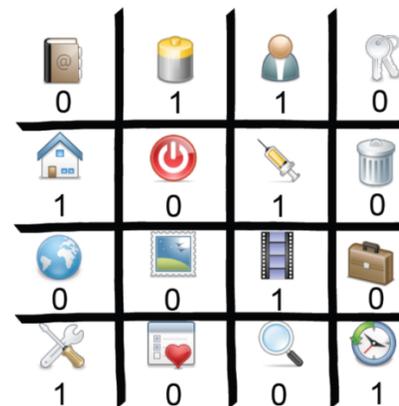
- Generate challenges without distinguishing between pass- and decoy objects
  - Rand-Rule: select  $l$  objects at random
  - Each object appears with the same probability  $p$  ( $l$  will be session varying if  $p < 1$ )
- Flip the response by a hidden bit (challenge)
  - The (binary) response is flipped according to a random hidden bit (which can be seen as a hidden challenge).
  - This makes responses independent of the number of pass-objects present in the challenge.
- If the response is not binary, the random hidden bit will be replaced by a random hidden variable.

# How to generate the random hidden bit?

- Ideally, an out-of-band (OOB) channel can be used.
  - This idea was proposed by some other researchers at CHI 2008 to design a solution based on hidden challenges.
- If an OOB channel is not acceptable or impossible, the flip bit has to be hidden in a public challenge.
  - Below is an example for Foxtail.



First challenge



Second (or flip-bit) challenge

## A fix to the fix

- The implementation of the fix without an OOB channel is actually still insecure.
  - The adversary can guess the position of the flip bit.
  - If the guess is wrong, nothing happens.
  - If the guess is correct, it will contribute to the frequency difference between pass- and decoy objects.
  - Experimentally validated, so a real threat.
- A possible fix to the fix
  - Use  $m > 1$  flip bits instead of just one.
  - When  $m = k$ , the adversary will have to guess the whole password so have no advantage by guessing the  $m$  bits.
  - Usability suffers: authentication time will be increased.

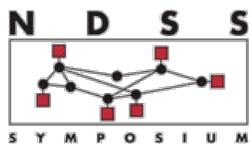
# Yet another (less generic) fix to Foxtail protocol (1)

- Foxtail 2.1: The fixed Foxtail protocol
  - All objects appear in each challenge.
  - Each object is assigned a random weight in  $\{0,1,2,3\}$ .
  - The response function is changed to the sum of the weights of all pass-objects mod 4.
- Is this enhanced Foxtail secure?
  - Secure against  $\delta D$  RIFA for any  $1 \leq \delta \leq k$ .
  - Secure against  $\delta D$  RDFFA when  $\delta < k$ .
  - “Insecure” against  $kD$  RDFFA, but in this case the attacking complexity is the same as brute forcing the password.  $\Rightarrow$  Secure against  $kD$  RDFFA as well.
- Usability suffers: challenges are large.

# Yet another (less generic) fix to Foxtail protocol (2)

- Foxtail 2.2: The fixed Foxtail protocol
  - Only  $l$  objects appear in each challenge.
  - Rand-Rule is used to select the  $l$  objects.
  - The response function is changed to the sum of the weights of all pass-objects mod 4.
- Is this enhanced Foxtail secure?
  - Secure against  $\delta D$  RIFA for any  $1 \leq \delta \leq k$ .
  - Theoretically insecure against  $\delta D$  RDFFA for any  $1 \leq \delta \leq k$ .
  - More than 2,000 authentication sessions are needed to launch a successful attack when  $(n, k, l) = (140, 14, 20)$ .  $\Rightarrow$  Practically secure!
- Usability improves: challenges are smaller.

- At NDSS 2012 Yan et al. also proposed a framework for estimating usability of human authentication protocols without running any real user study.
- The estimated authentication times
  - Original insecure Foxtail: 213 seconds
  - Foxtail 2.1: 475 seconds
  - Foxtail 2.2: 274 seconds
- Foxtail 2.2 is practical secure and slightly less usable than the original Foxtail.
- Open questions for future work: **1) are there other attacks to Foxtail 2.x? 2) how can we do better?**



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Thanks for your attention!

Contact the authors for questions:

[hassan.asghar@mq.edu.au](mailto:hassan.asghar@mq.edu.au)

[shujun.li@surrey.ac.uk](mailto:shujun.li@surrey.ac.uk)

[ron.steinfeld@monash.edu](mailto:ron.steinfeld@monash.edu)

[josef.pieprzyk@mq.edu.au](mailto:josef.pieprzyk@mq.edu.au)