

# Indiscreet Logs: Diffie-Hellman Backdoors in TLS

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Discrete logarithms are “easy” in smooth order groups... if you know the factorization of the group order.

What if you don't know the group order? What if it was hidden somehow?

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What if you don't know the group order? What if it was hidden somehow?

The discrete logarithm problem *could* be hard. Or it could be easy. So which one is it?

What if it was manufactured to be easy, and only the attacker can tell?

# Outline

What is the **vulnerability**?

How is it **possible**?

How do we **force DH** use?

What are the **attack vectors**?

**How many** did we find?

What **disclosures** did we do?

**What can be done** to prevent this?

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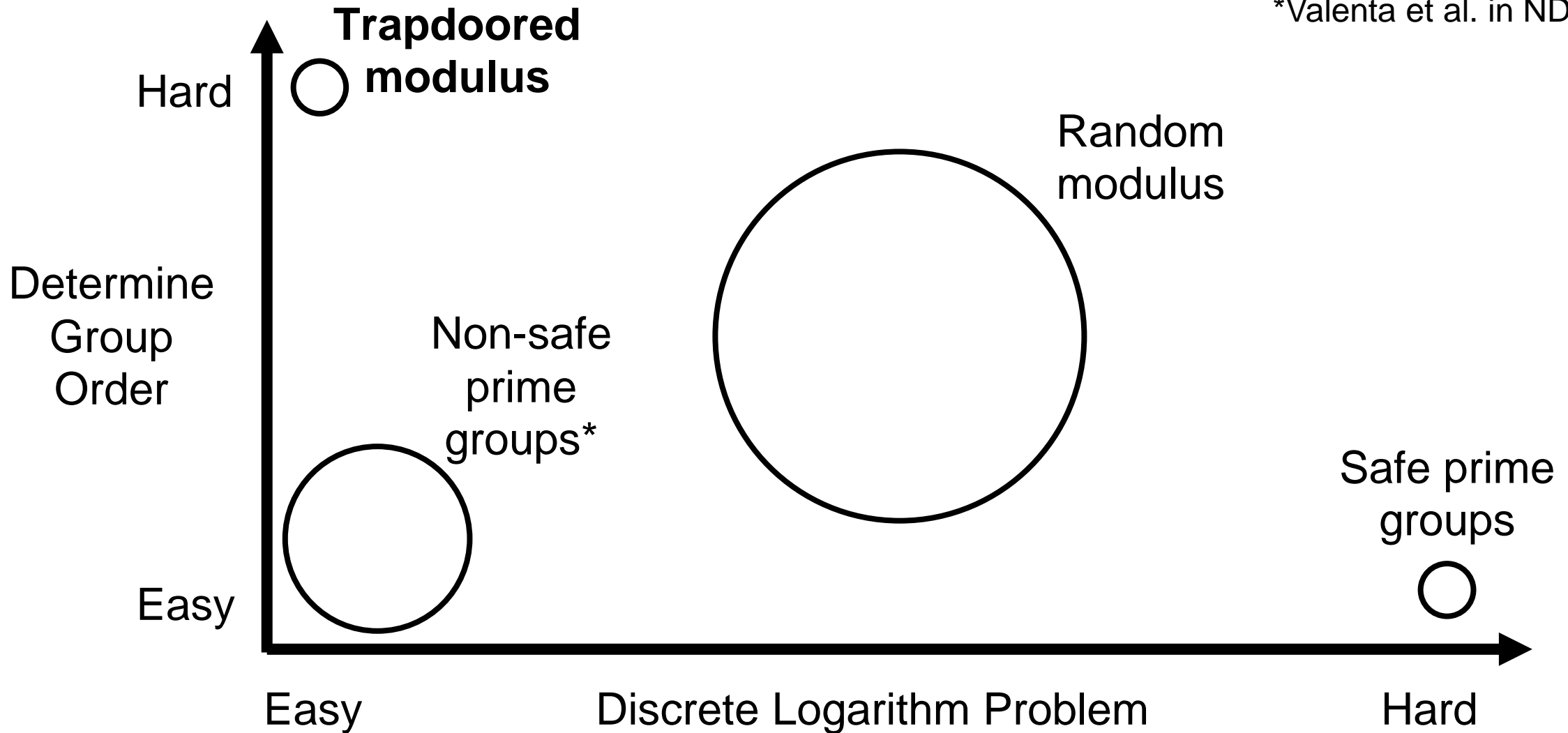
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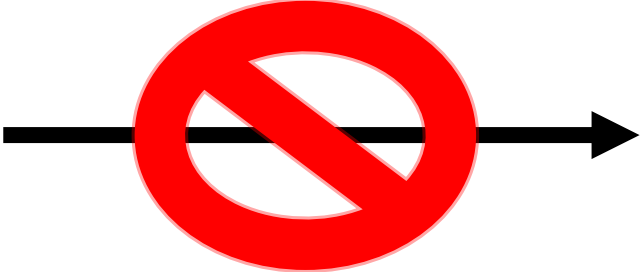
# Exploiting Small and Smooth Order Subgroups

\*Valenta et al. in NDSS 2017



Trapdoor  Composite Modulus

Trapdoor  Composite Modulus

Composite Modulus  Trapdoor



Composite Modulus:

Mistake...or trapdoor?

Can't tell unless you factor modulus

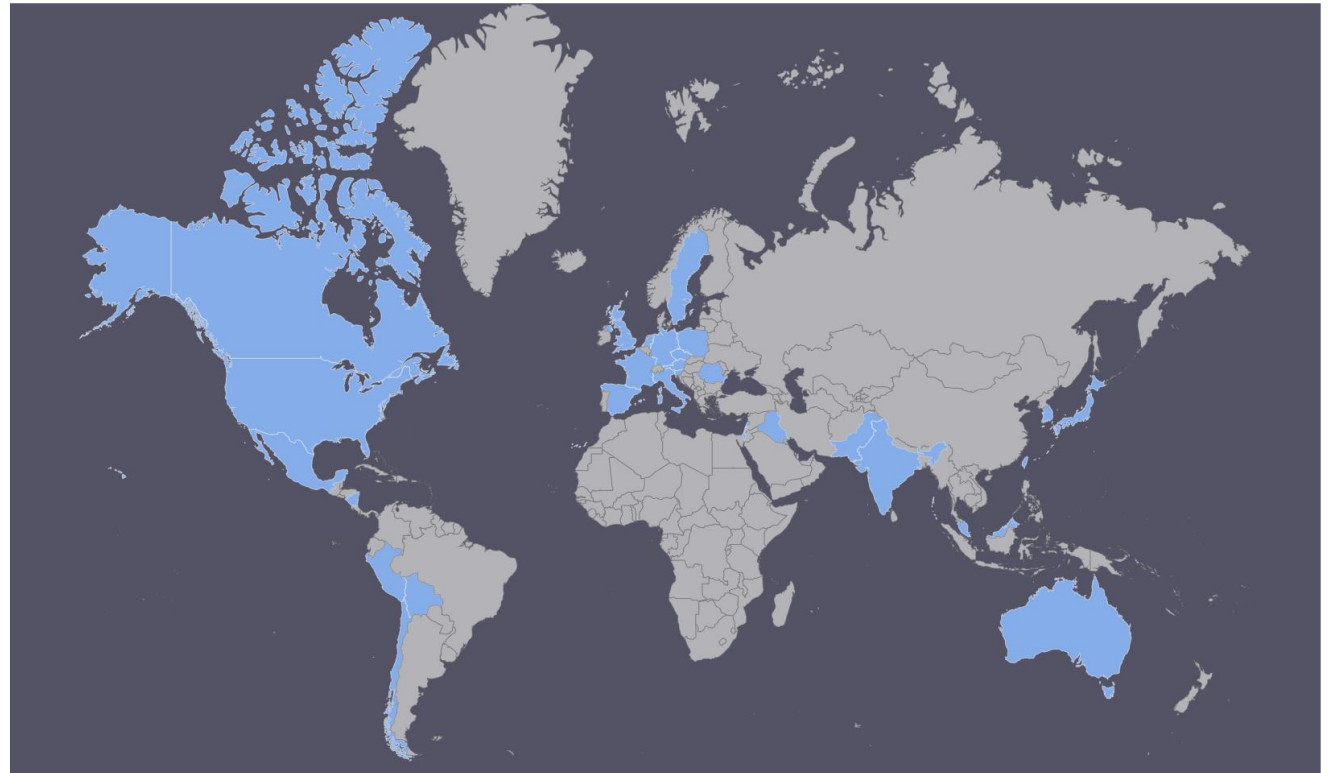
# Vulnerability

## The Vulnerability

- Composite DH moduli used in TLS and STARTTLS
- 30+ countries
- 20+ companies

## Implications of Trapdoors

- Shared secret recovery
- Passive eavesdropping
- Traffic modification



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# How Is This Possible?

Systematically poor parameter validation by discrete logarithm implementations

Primality not checked  
Why not?

Primality testing is “math fast” but not “Internet fast”

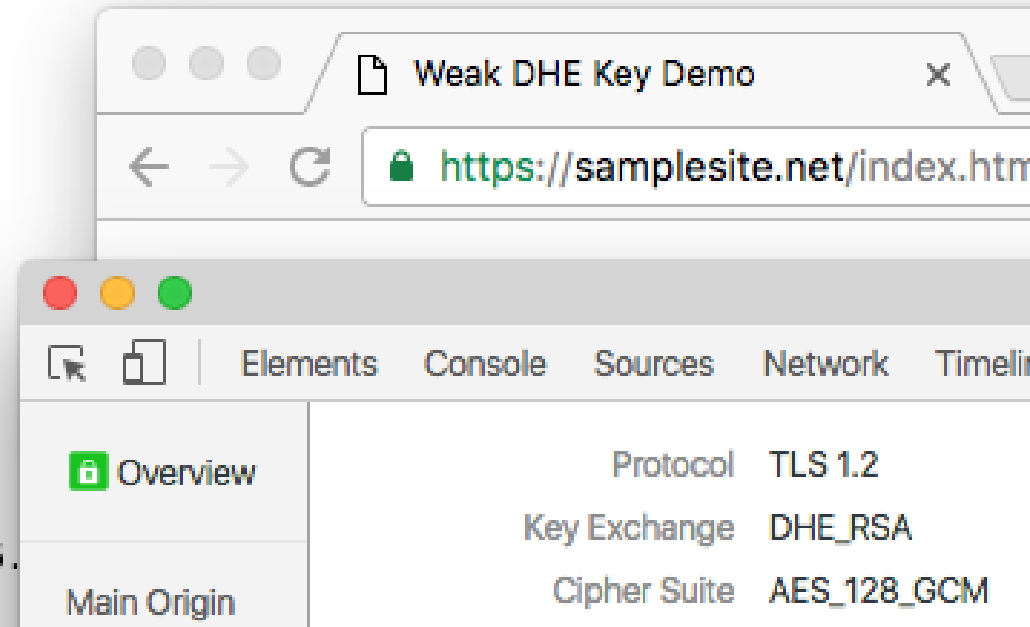
# Chrome Connection

Subgroup of order 3

```
▼ Handshake Protocol: Server Key Exchange
  Handshake Type: Server Key Exchange (12)
  Length: 1290
▼ Diffie-Hellman Server Params
  p Length: 256
  p: ffffffffffffffffffffffffffffffffffffffffffffffffffffffff...
  g Length: 256
  g: 99c68595375f92606c26d55a8ecbf93be2d0636800cc7bc...
  Pubkey Length: 256
  Pubkey: 99c68595375f92606c26d55a8ecbf93be2d0636800cc7bc...
  Signature Hash Algorithm: 0x0601
  Signature Length: 512
  Signature: led2a04061d6df57b350070b8dd84d2ad42d678f249b4c6...
TLSv1.2 Record Layer: Handshake Protocol: Server Hello Done
```

Not prime

Private Key = 1



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# Forcing DHE

DHE used in <1% TLS connections but still (somewhat) widely supported

Small subgroups allow attacker to compute master secret

“Downgrade” attack to force DHE ciphersuites for TLS 1.2 and below

Downgrade protections in TLS 1.3 prevent this attack

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# Getting Weak Parameters Used Three attack vectors

## 1. Drop onto server



With Root Access

Weak DH  
Parameters



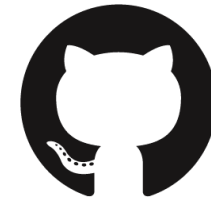
# Getting Weak Parameters Used

Three attack vectors

## 2. Incorporate into open-source project



Patch



**GitHub**

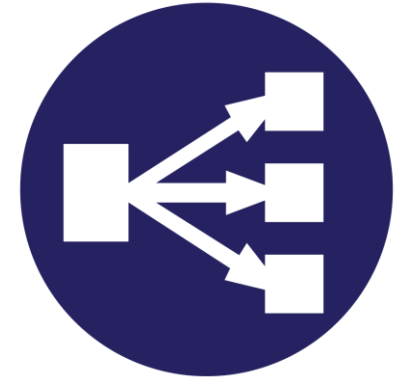
# Getting Weak Parameters Used

Three attack vectors

## 3. Install onto network appliance before shipment



Weak DH  
Parameters



Company Employee

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# How Many Weak Parameters Did We Find?

43M IPs using HTTPS, 11M supporting DH

## Composite Moduli

- 280 IPs in HTTPS
- 272 IPs in IMAPS, POP3S, SMTPS, SMTP
- Private key recoveries up to 42% of length



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## Non-safe Prime Moduli\*

- 1.6M IPs in HTTPS
- Private key recoveries up to 50% of length

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# Disclosures



## Companies

- 56% fixed vulnerability
- 19% in progress
- 25% unchanged

## Solutions

- Change to prime moduli
- Remove DHE ciphersuites



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# How Do We Stop It From Occurring?

- Deprecating DH ciphersuites
- Verifying DH parameters correctly
- Use named parameters like for ECDHE
- Sign all previously exchanged messages in ServerKeyExchange



# Takeaway Points

Composite moduli of unknown order exist on the Internet today

Could be trapdoored moduli allowing man-in-the-middle attacks,  
or could just be benign carelessness

**We can't tell and they can't say**

**Thank You!**  
**Questions?**

