Constant Round Maliciously Secure 2PC with Function-independent Preprocessing using LEGO

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Abstract-Secure two-party computation (S2PC) allows two parties to compute a function on their joint inputs while leaking only the output of the function. At TCC 2009 Orlandi and Nielsen proposed the LEGO protocol for maliciously secure 2PC based on cut-and-choose of Yao's garbled circuits at the gate level and showed that this is asymptotically more efficient than on the circuit level. Since then the LEGO approach has been improved upon in several theoretical works, but never implemented. In this paper we describe further concrete improvements and provide the first implementation of a protocol from the LEGO family. Our protocol has a constant number of rounds and is optimized for the offline/online setting with function-independent preprocessing. We have benchmarked our prototype and find that our protocol can compete with all existing implementations and that it is often more efficient. As an example, in a LAN setting we can evaluate an AES-128 circuit with online latency down to 1.13 ms, while if evaluating 128 AES-128 circuits in parallel the amortized cost is 0.09 ms per AES-128. This online performance does not come at the price of offline inefficiency as we achieve comparable performance to previous, less general protocols, and significantly better if we ignore the cost of the function-independent preprocessing. Also, as our protocol has an optimal 2-round online phase it is significantly more efficient than previous protocols when considering a high latency network.

Keywords—Secure Two-party Computation, Implementation, LEGO, XOR-Homomorphic Commitments, Selective OT-Attack

I. INTRODUCTION

Secure two-party computation is the area of cryptology dealing with two mutually distrusting parties wishing to compute an arbitrary function f on private inputs. Say A has

NDSS '17, 26 February - 1 March 2017, San Diego, CA, USA Copyright 2017 Internet Society, ISBN 1-891562-46-0 http://dx.doi.org/10.14722/ndss.2017.23075 input x and B has input y. The guarantee offered from securely computing f is that the only thing learned from the computation is the output z = f(x, y), in particular nothing is revealed about the other party's input that cannot be inferred from the output z. This seemingly simple guarantee turns out to be extremely powerful and several real-world applications and companies using secure computation have arisen in recent years [1]-[3], [15], [16]. The idea of secure computation was initially conceived in 1982 by Andrew Yao [70], [71], particularly for the *semi-honest* setting, in which all parties are assumed to follow the protocol specification but can try to extract as much information as possible from the protocol execution. Yao gave an approach for preventing any such extraction using a technique referred to as the garbled circuit technique. At a very high level, using the abstraction of [12], A starts by garbling or "encrypting" the circuit f using the garbling algorithm $(F, e, d) = \mathsf{Gb}(f)$ obtaining a garbled circuit F, an input encoding function e and an output decoding function d. It then encodes its input as X = En(x, e) and sends (F, X, d) to B. Then, using oblivious transfer (OT), A blindly transfers a garbled version Y of B's input which enables B to compute a garbled output $Z = \mathsf{Ev}(F, X || Y)$ which it can then decode to obtain z = De(Z, d). Finally B returns z to A.

As already mentioned, the above sketched approach can be proven secure in the semi-honest setting [52]. In the stronger malicious setting however it completely breaks down as in this model the parties are allowed to deviate arbitrarily from the protocol specification. One of the most obvious attacks is for A to garble a different function $f' \neq f$ which could enable A to learn y from the resulting value z' without B even noticing this. To combat this type of attack the cut-and-choose technique can be applied: instead of garbling a single circuit, A garbles several copies and sends these to B. A random subset of them is now selected for checking by B and if everything is correct, some fraction of the remaining circuits must be correct with overwhelming probability. Leaving out many details these can now be evaluated to obtain a single final output. While this approach thwarts the above attack it unfortunately opens up for several new ones that also need to be dealt with, for instance ensuring input consistency for all the remaining evaluation garbled circuits. Another more subtle issue in the malicious setting is the Selective-OT Attack (also called Selective Failure Attack) as pointed out in [46], [57]. A corrupt A can cheat when offering B the garbled inputs in the OT step by using a bogus value for either the 0 or the 1 input. This will either result in B aborting as it cannot evaluate the garbled circuit or it will go through undetected and B will return the output to A. Either way the input bit of B is revealed to A which is a

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	Sec	eret Sharing	-based		Garble	d Circuit-base	ed
Protocol	[45]*	[28]*	[26]*	[69]	[56]	[65]	This Work
Constant round	×	×	×	\checkmark	\checkmark	\checkmark	\checkmark
Independent preprocessing	N/A	×	×	X	X	×	$13.84\mathrm{ms}$
Dependent preprocessing	×	N/A	N/A	$62\mathrm{ms}$	$74\mathrm{ms}$	$5.1\mathrm{ms}$	$0.74\mathrm{ms}$
Best online latency	$12\mathrm{ms}$	$6\mathrm{ms}$	$1.05\mathrm{ms}$	21 ms	$7\mathrm{ms}$	$1.3\mathrm{ms}$	$1.13\mathrm{ms}$
Best online throughput	${\sim}1{\rm ms}$	$0.4\mathrm{ms}$	$0.45\mu s$	N/A	N/A	$0.26\mathrm{ms}$	$0.08\mathrm{ms}$

*Uses dedicated techniques for evaluating AES.

TABLE I.Overview of state-of-the-art protocols and the best reported timings for securely evaluating AES-128 with malicious
security on a LAN in the offline/online setting. All timings are per AES-128. N/A stands for Not Available.

direct breach of security. It is easy to see that using this attack A can learn any l bits of B's input with probability 2^{-l} if not properly dealt with.

Over the last decade several solutions to the above issues have been proposed, along with dramatic efficiency improvements for secure 2PC protocols based on the cut-and-choose approach of garbled circuits [4], [18], [32], [36], [39], [40], [42], [48], [50], [51], [53], [58], [64], [66], [67], [69]. Finally we note for completeness that secure computation has also been studied in great detail for many other settings, including the more general multi-party case (MPC). Several different adversarial models such as honest majority [14], [22], [37], dishonest majority [27] and covert security [7] have also been proposed in the literature. In this work we focus solely on the special case of two parties with malicious security and in the next section we discuss the reported concrete efficiency of state-of-the-art protocols in this setting.

A. Related Work

In the less than 10 years since the first reported implementation of maliciously secure 2PC based on garbled circuits [54], the performance advancements have been enormous [4], [32], [36], [48], [56], [64]–[67], [69]. Furthermore different settings and hardware configurations have been explored, notably using commodity grade GPUs in [32], [36] and large-scale CPU clusters [67] to parallelize the bulk of the computation. In the single-execution setting based solely on standard hardware the best reported performance time is that of [69] which evaluates an AES-128 circuit in total time 65 ms. In addition, the works of [56] and [65] explore the more restricted setting of amortizing secure 2PC based on the cut-and-choose and the dual execution approach, respectively. By amortizing we mean that the protocols exploit constructing multiple secure evaluations of the same function f yielding impressive performance benefits over the more general single execution setting. Furthermore these protocols are in the offline/online setting where the bulk of the computation and communication can be done before the inputs are determined. We highlight that for both protocols, the offline computation depends on the function to be computed and we will refer to this as dependent preprocessing. However both protocols allow for the inputs to be chosen sequentially when securely evaluating f. This allows for a low latency online phase which is desirable for many applications. For securely computing 1024 AES-128 circuits, [56] reports 74 ms offline and 7 ms online per evaluation, while the more recent [65] reports 5.1 ms offline and 1.3 ms online for the same setting. Furthermore [65] achieves a 0.26 ms online phase when considering throughput alone, i.e. batched evaluation.

Another direction in secure computation is the secret sharing approach where the parties initially secret share their inputs and then interactively compute the function f in a secure manner. A particularly nice property of these protocols is that when considering the offline/online setting the offline phase can usually be done independently of the circuit fwhich we call independent preprocessing. This allows for naively utilizing parallelism in the preprocessing phase and also adds more flexibility as the offline material produced is universal. Another benefit is that in general this secretsharing technique works for any number of parties and over any field, which depending on the desired functionality f can significantly increase performance. We note however that these protocols usually employ expensive public-key cryptography in the preprocessing phase and are therefore much slower than the offline phases of e.g. [56], [65]. Finally the inherent interactiveness of the online phase, which has $\mathcal{O}(\mathsf{depth}(f))$ rounds of interaction, makes these protocols ill-suited for high latency networks such as WANs. There are many variations of the secret sharing approach but they typically enjoy the same overall pros and cons in terms of independent preprocessing and required interactivity. Examples of recent protocols following this paradigm are: TinyOT [19], [49], [60], SPDZ [24], [27], [44], [45], MiniMac [25], [28], [29], and TinyTables [26]. The fastest reported online time for computing an AES-128 circuit in this setting is 1.05 ms by [26] using dependent preprocessing. The work of [45] reports 12 ms online time using independent preprocessing, but the evaluation exploits the algebraic structure of AES-128. Furthermore [26] has an impressive throughput of 0.45 µs per AES-128 while [45] and [28] have throughput $\sim 1 \,\mathrm{ms}$ and $0.4 \,\mathrm{ms}$, respectively.

In Table I we give an overview of the properties of the mentioned protocols and the reported timings for securely evaluating AES-128 on LAN in the offline/online setting. As the secret sharing-based, non-constant round, protocols are illsuited for high latency networks we omit this from Table I since no AES-128 timings are published for these schemes in a WAN setting (however see Section VI-B for a WAN comparison of the garbled circuit protocols). The timings reported for [26], [56], [65] and This Work are all measured on the same hardware (Amazon Web Services, c4.8xlarge instances on 10 Gbit LAN), while the timings for [69] are on a less powerful instance (Amazon Web Services, c4.2xlarge instances on 2.5 Gbit LAN). Finally the results of [28], [45] have been obtained on high-end Desktop machines with 1 Gbit LAN. The timings of [56], [65] and This Work are all for 1024 AES-128 evaluations, while those of [69] are for a singleexecution. We believe the difference in performance between the offline/online (62 ms + 21 ms) and total latency (65 ms)

settings for [69] can be explained by the inability to interleave the sending/checking and evaluation of garbled circuits in the offline/online setting. In summary, as can be seen in the table our work is the first implementation of a protocol combining the advantages of independent (and dependent) preprocessing using only a constant number of rounds.

B. LEGO

The Large Efficient Garbled-circuit Optimization (LEGO) was first introduced by Nielsen and Orlandi in [61] which showed a new approach for maliciously secure 2PC based on cut-and-choose of garbled gates. This gave an asymptotic complexity improvement to $\mathcal{O}(s/\log(|f|))$ as opposed to $\mathcal{O}(s)$ for the standard *circuit* cut-and-choose approach for statistical security s. However the construction of [61] was heavily based on expensive public-key cryptography and was mainly considered an asymptotic advancement. This was later improved in the two follow-up works of MiniLEGO [35] and TinyLEGO [33] yielding incrementing asymptotic and concrete efficiency improvements. In a nutshell, the LEGO technique works by the generator A first garbling multiple individual AND gates (as opposed to garbling entire circuits) and sending these to the evaluator B. Then a cut-and-choose step on a random subset of these gates is carried out and finally the remaining unchecked gates are combined (or soldered) into a garbled fault tolerant circuit computing f. A crucial ingredient for securely soldering the garbled gates into circuits are XOR-homomorphic commitments which in [61] were realized using expensive Pedersen commitments [62]. In the follow-up construction of [35] these were replaced by an asymptotically more efficient construction, however the concrete communication overhead of the proposed commitment scheme was inadequate for the protocol to be competitive for realistic circuit sizes and parameters. In the recent works of [21], [34] this overhead has been improved to an optimal rate-1 and the resulting UC-secure XOR-homomorphic commitment scheme is both asymptotically and concretely very efficient. Finally the work of [41] introduced a different primitive for LEGO soldering called XOR-Homomorphic Interactive Hash, which has some advantages over the commitment approach. However, the best instantiation of XOR-Homomorphic Interactive Hash still induces higher overall overhead than the commitment approach when using the schemes of [21], [34].

Although the original LEGO protocol, and the abovementioned follow-up works, asymptotically are very efficient, the overall consensus in the secure computation community has been that the reliance of XOR-homomorphic commitments for all circuit wires hinders actual practical efficiency. In this work we thoroughly investigate the practical efficiency of the LEGO approach and, in contrast to earlier beliefs, we demonstrate that it is indeed among the most practical protocols to date for general secure 2PC using garbled circuits.

C. Our Contributions

We implement the TinyLEGO protocol with added support for both independent and dependent preprocessing. Furthermore, our protocol supports fully reactive computation, meaning that when a function result has been obtained, another function depending on this result can be evaluated. Also, the independent preprocessing phase can be rerun at any

Setting	Ind. Preprocessing*	Dep. Preprocessing	Online Latency	Online Throughput
Single Execution 1 x AES-128 1 x SHA-256	$\begin{array}{c} 89.61\mathrm{ms}\\ 478.54\mathrm{ms} \end{array}$	$\begin{array}{c} 13.23\mathrm{ms}\\ 164.40\mathrm{ms} \end{array}$	$\begin{array}{c} 1.46\mathrm{ms} \\ 11.19\mathrm{ms} \end{array}$	$\begin{array}{c} 1.46\mathrm{ms} \\ 11.19\mathrm{ms} \end{array}$
Amortized 128 x AES-128 128 x SHA-256	$\begin{array}{c} 14.85\mathrm{ms}\\ 173.05\mathrm{ms} \end{array}$	0.68 ms 12.13 ms	$\begin{array}{c} 1.15\mathrm{ms}\\ 9.35\mathrm{ms} \end{array}$	$\begin{array}{c} 0.09\mathrm{ms}\\ 1.09\mathrm{ms} \end{array}$
"Not including the	time to compute t	he initial BaseOTs	s.	

TABLE II.	PERFORMANCE SUMMARY OF OUR PROTOCOL ON A HIGH
	BANDWIDTH (10GBIT) LAN NETWORK.

time if additional garbling material is necessary. As part of our prototype we also implement the XOR-homomorphic commitment scheme of [34] and report on its efficiency separately as we believe our findings can be of independent interest. This is to our knowledge the first implementation of a protocol based directly on the LEGO paradigm and of the mentioned commitment scheme. The support for independent preprocessing is achieved from the fact that the bulk of the computation using the LEGO approach is based on cut-andchoose of independently garbled gates and hence only depends on the security parameter and the number of AND gates one wishes to preprocess. The subsequent soldering phase can then be seen as a dependent preprocessing phase where knowledge of the circuit f is required. This multi-level preprocessing is in contrast to previous non-LEGO protocols based on cut-andchoose of garbled circuits in the offline/online setting where the entire offline phase depends on the circuit to be evaluated. In more detail our main contributions are as follows:

- 1) We propose a new technique for dealing with the selective-OT attack on 2PC protocols based on garbled circuits. Our technique makes use of a globally correlated OT functionality ($\mathcal{F}_{\Delta-ROT}$) combined with XORhomomorphic commitments and a Free-XOR garbling scheme [47]. Using the well-known fact of Beaver [8] that OTs can be precomputed, we can mitigate the selective-OT attack by having the circuit constructor decommit to a single value per input bit of the evaluator in the online phase. This ensures that if the constructor tries to cheat, the evaluator aborts regardless of the value of his input. The technique is general and we believe that it can be used in other 2PC protocols based on garbled circuits as well. We also provide a more efficient instantiation of $\mathcal{F}_{\Delta-\mathsf{ROT}}$ than previously appearing in the literature by tightening the analysis of the construction presented in [19].
- 2) As part of our 2PC prototype we also implement the XOR-homomorphic commitment scheme of [34]. It is already known that this scheme is asymptotically very efficient, but this is to our knowledge the first time its practical efficiency has been thoroughly investigated. The result is a very efficient scheme achieving an amortized cost of less than a microsecond for both committing and decommitting to a random value. To maximize performance we utilize cache efficient matrix-transposition and inspired by the construction of [21] we use the Intel Streaming SIMD Extension (SSE) instruction PCLMULQDQ to efficiently compute the required linear combinations.
- 3) We build our LEGO prototype on top of the abovementioned implementation which results in a very effi-

cient and flexible protocol for maliciously secure reactive 2PC. As our online phase consists of an optimal two rounds, we can securely evaluate an AES-128 with latency down to $1.13 \,\mathrm{ms}$. When considering throughput we can do each AES-128 block in amortized online time $0.08 \,\mathrm{ms}$ (considering 1024 blocks). In applications where independent preprocessing can be utilized our offline phase is superior to all previous 2PC protocols, in particular based on our experiments we see a 6-54x gain over [65] depending on network and number of circuits considered. If preprocessing is not applicable, for most settings we cannot compete with the offline phase of [65], but note that the difference is within a factor 1.2-3x. See Table II for an overview of our performance in different settings and Section VI for a more detailed presentation and comparison of our results.

II. PRELIMINARIES

In this section we give some of the technical background for LEGO garbling, adopting the notation and conventions of the original TinyLEGO protocol [33] for ease of exposition.

A. Notation

We will use as shorthand $[n] = \{1, 2, ..., n\}$ and $[i; j] = \{i, i + 1, i + 2, ..., j\}$. We write $e \in_R S$ to mean: sample an element e uniformly at random from the finite set S. We sometimes (when the semantic meaning is clear) use subscript to denote an index of a vector, i.e., x_i denotes the i'th bit of a vector x. We use k to denote the computational security parameter and s to represent the statistical security parameter. Technically, this means that for any fixed s and any polynomial time bounded adversary, the advantage of the adversary is $2^{-s} + \operatorname{negl}(k)$ for a negligible function negl. i.e., the advantage of any adversary goes to 2^{-s} faster than any inverse polynomial in the computational security parameter. If $s = \Omega(k)$ then the advantage is negligible. In our experiments we set k = 128 and s = 40.

B. Circuit Conventions

We assume A is the party constructing the garbled gates and call it the *constructor*. Likewise, we assume B is the party evaluating the garbled gates and call it the *evaluator*. Furthermore, we say that the functionality they wish to compute is z = f(x, y), where A gives input x and B gives input y. We assume that f is described using only NOT, XOR and AND gates. The XOR gates are allowed to have unlimited fan-in, while the AND gates are restricted to fan-in 2, and NOT gates have fan-in 1. All gates are allowed to have unlimited fan-out. We denote the bit-length of x by $|x| = n_A$, the bit-length of y by $|y| = n_B$ and let $n = n_A + n_B$. We will denote the bitlength of the output z by |z| = m. Furthermore, we assume that the first n_A input wires are for A's input and the following n_B input wires are for B's input.

We define the *semantic* value of a wire-key of a garbled gate to be the bit it represents. We will use K_j^b to denote the j'th wire key representing bit b. Sometimes, when the context allows it, we will let $L_g^{b_l}$, $R_g^{b_r}$, and $O_g^{b_o}$ denote the left input, right input, and output key respectively for garbled gate g representing the bits b_l , b_r and b_o . When the bit represented by a key is unknown we simply omit the superscript, e.g. K_j .

C. Free-XOR and Soldering

The LEGO protocols [35], [61] and [33] all assume that the underlying garbling scheme supports the notion of Free-XOR [47], meaning that the XOR of the 0- and 1-key on any wire of any garbled gate yields the same value, Δ , which we call the *global difference*. In addition to making garbling and evaluating XOR gates virtually free, this optimization also allows for easily soldering wires together. A soldering of two wires is a way of transforming a key representing bit *b* on one wire into a key representing bit *b* on the other wire. As we will see in more detail below, with Free-XOR, a soldering is simply the XOR of the 0-keys on the two wires. Furthermore, in order to avoid any cheating all wires of all garbled gates are committed to using a XOR-homomorphic commitment functionality $\mathcal{F}_{\text{HCOM}}$ and the solderings are then always decomitted when needed.

As an example, assume we wish to solder the output wire of gate g onto the left input wire of gate g + 1. In doing so we decommit the value $S_{g+1}^L = O_g^0 \oplus L_{g+1}^0$ using $\mathcal{F}_{\text{HCOM}}$. When gate g outputs the key representing the bit b one can now learn the left b-key for gate g + 1. Specifically it can be computed as $O_g^b \oplus S_{g+1}^L = (O_g^0 \oplus (b \cdot \Delta)) \oplus O_g^0 \oplus L_{g+1}^0 = L_{g+1}^0 \oplus (b \cdot \Delta) = L_{g+1}^b$. This obviously generalizes when one wishes to solder together several wires, e.g. if we wish to solder the output wire of gate g to the left input wire of gate g + 1, g + 2 and g + 3, then it is enough to decommit the values $S_{g+1}^L = O_g^0 \oplus L_{g+1}^0, S_{g+2}^L = O_g^0 \oplus L_{g+2}^0, S_{g+3}^L = O_g^0 \oplus L_{g+3}^0$.

It is also straightforward to evaluate XOR gates as part of the soldering: To compute the XOR of g and g + 1 and then use this result as the left input to gate g + 2 we decommit the value $S_{g+2}^L = (O_g^0 \oplus O_{g+1}^0) \oplus L_{g+2}^0$. We see now that $O_g^a \oplus O_{g+1}^b \oplus S_{g+2}^L = a \cdot \Delta \oplus b \cdot \Delta \oplus L_{g+2}^0 = L_{g+2}^{a \oplus b}$ as desired. In conclusion a soldering is therefore always the XOR of the 0-keys of the wires going into an XOR gate and the 0-key of the wire we wish to solder the result onto.

III. A NEW APPROACH TO ELIMINATE THE SELECTIVE-OT ATTACK

As already mentioned in Section I the selective-OT attack enables a corrupt A to learn any input bit of B with success probability 1/2 for each bit. Prior work has dealt with this attack in different ways, but the off-the-shelf blackbox solution has typically been the s-probe resistant matrix approach of [51], [56], [67]. These approaches augment the evaluation circuit $f \rightarrow f'$ so that learning any s-1 input bits of B in f' leaks nothing about the actual input used in the original f. The downside of this approach is that the input length of B needs to be increased to $n'_{\rm B} > n_{\rm B}$, which in turn results in more communication, computation and OTs. For the approach of [51] and [56] the increase is to $n'_{\mathsf{B}} = n_{\mathsf{B}} + \max(4n_{\mathsf{B}}, \frac{20s}{3})$ while for the approach of [67] we have $n'_{\mathsf{B}} \le n_{\mathsf{B}} + \lg(n_{\mathsf{B}}) + n_{\mathsf{B}} + s + s \cdot \max(\lg(4n_{\mathsf{B}}), \lg(4s))$. In addition to extending the input size, experiments of [56] show that producing the s-probe resistant version of f can be a computationally expensive task (up to several seconds for 1000-bit input).

A. Our New Approach

We propose a new approach that combines the use of 1out-of-2 Δ -ROTs (also called globally correlated OTs), XORhomomorphic commitments and the Free-XOR technique that sidesteps the need of expanding the input size of B as described above. We recall that Δ -ROTs are similar to Random OTs (ROT), except that all OTs produced are correlated with a global difference Δ . In other words, for each Δ -ROT *i* produced, the following relation holds for a fixed Δ : $r_i^1 = r_i^0 \oplus \Delta$ where $r_i^0, \Delta \in \{0, 1\}^k$ are uniformly random strings known to the sender and $b_i \in \{0, 1\}$ is the uniformly random choice-bit of the receiver who learns $r_i^{b_i}$ as part of the OT protocol. Our approach is described below and is inspired by the protocol of Beaver [8] for precomputing OT.

- 1) The parties precompute $(n_{\rm B}+s)$ $\Delta\text{-ROTs}$ such that the sender learns (Δ, r_i^0) and the receiver learns $(r_i^{b_i}, b_i)$ for $i \in [n_{\mathsf{B}}+s]$. The sender will now commit, using the XORhomomorphic commitment scheme, to Δ and each r_i^0 . In order to verify that the sender indeed committed to the Δ used in the OTs, the parties run a simple check in the following way: B sends $\{(r_j^{b_j}, b_j)\}_{j \in [n_{\mathsf{B}}; n_{\mathsf{B}}+s]}$ to A which in turn needs to successfully decommit to the received values. The s OTs used for the check are hereafter discarded. The reason why B needs to send the values to A in the first place is that it needs to prove knowledge of the value $r_j^{b_j}$ before it is safe for A to open it. For each of the s tests, if A did not commit to the Δ used in the OTs, then it can only pass the test with probability at most 1/2as the choice-bits of B are uniformly random. Because these are also chosen independently we see that the check therefore catches a cheating A with overwhelming probability $1-2^{-s}$.
- 2) If the check succeeds, A uses the Δ learned from the OTs above as the global difference in the Free-XOR garbling scheme. Recall that this means that all garbling keys will be correlated in the same way as the Δ -ROTs, i.e. $K_l^1 = K_l^0 \oplus \Delta$ for all *l*. In particular this is the case for the keys associated to the input of B which need to be obliviously transferred in the online phase. In addition, in our 2PC protocol all 0-keys K_l^0 have been committed to using the same XOR-homomorphic commitment scheme as used for the OT strings r_i^0 and Δ .
- Finally when B learns its real input y, it computes e = y ⊕ b and sends this to A where b are the choicebits used in the precomputed Δ-ROTs. A will respond by decommitting the values {D_i = K_i⁰ ⊕ r_i^{e_i}}_{i∈[n_B]}. B can now compute its actual input keys K_i^{y_i} = D_i ⊕ r_i<sup>b_i</sub> = K_i⁰ ⊕ r_i^{e_i} ⊕ r_i^{b_i} = K_i⁰ ⊕ y_i · Δ.
 </sup>

The above approach eliminates the selective-OT attack as the only way a corrupt A can cheat is by committing to different values $r'_i^0 \neq r_i^0$ where r_i^0 is the value sent using the Δ -ROTs. However if this is the case then $D'_i \oplus r_i^{b_i} \notin \{K_i^0, K_i^1\}$ and B will abort regardless of the value of his input y_i . One caveat of the above approach is that it allows a corrupt A to flip an input bit *i* of B without getting caught by committing to $r_i^0 \oplus \Delta$ instead of r_i^0 . In our 2PC protocol we eliminate this issue by ensuring that $lsb(\Delta) = 1$ and by securely leaking $lsb(r_i^0)$ to B. This allows B to check that the resulting key $K_i = D_i \oplus r_i^{b_i}$

indeed carries the correct value y_i , by verifying that

$$y_i = \operatorname{lsb}(K_i) \oplus \operatorname{lsb}(D_i) \oplus \operatorname{lsb}(r_i^0) \oplus e_i$$

= $\operatorname{lsb}(K_i) \oplus \operatorname{lsb}(K_i^0) \oplus \operatorname{lsb}(r_i^{e_i}) \oplus \operatorname{lsb}(r_i^0) \oplus e_i$
= $\operatorname{lsb}(K_i) \oplus \operatorname{lsb}(K_i^0)$.

This secure leaking is described in the *VerLeak* step of Fig. 1 and the check is carried out as part of the **Eval** step of Fig. 2, both of which are presented in Section IV.

B. On Constructing Δ -ROTs

The above technique requires $(n_{\mathsf{B}} + s) \Delta$ -ROTs to obliviously transfer the input keys of B. However, current stateof-the-art protocols for OT extension [6], [19], [43], [60] all produce ROTs. It can be seen by inspecting the above OT extension protocols that they all produce a weaker variant of Δ -ROT called *leaky* Δ -ROT as an intermediate step. The leaky Δ -ROT is identical to Δ -ROT in that all OT pairs are correlated with a global Δ , however a corrupt receiver can cheat and learn some bits of Δ with non-negligible probability. In fact, for each bit learned of Δ , the receiver gets caught with probability 1/2, which means it can learn up to s-1 bits of Δ , while the other bits remain uniformly random in its view. The work of [19] gives a construction for Δ -ROTs of string length v from leaky Δ -ROTs of string length $22v/3 \sim 7.33v$ using linear randomness extraction. Concretely, they propose multiplying all the strings learned from the leaky Δ -ROT protocol with a random matrix $A \in \{0, 1\}^{22\nu/3 \times \nu}$. In this work we observe that the factor $\frac{22}{3}$ is not tight and by applying Theorem 1 below we can reduce the number of rows in Adown to v+s, going from a multiplicative to an additive factor.

Theorem 1 ([73], Theorem 7). Let $X = x_1, x_2, \ldots, x_u$ be a binary sequence generated from a bit fixing source in which l bits are unbiased and independent, the other u - l bits are fixed or copies of the l independent random bits. Let A be a $u \times v$ random matrix such that each entry of A is 0 or 1 with probability 1/2. Given Y = XA, then we have that

$$\Pr_A[\rho(Y) \neq 0] \le 2^{v-l}$$

where $\rho(Y)$ is defined as the statistical distance to the uniform distribution over $\{0,1\}^v$, i.e. $\rho(Y) = \frac{1}{2} \sum_{y \in \{0,1\}^v} |\Pr[Y = y] - 2^{-v}|$.

Now let u = v + s and let Δ have length u and let ΔA have length v. Consider an adversary B who is allowed to try to learn some of the bits of Δ to make ΔA non-uniform. In our setting, if an adversary B tries to learn λ bits of Δ it is caught except with probability $2^{-\lambda}$. If B is not caught then it learns λ bit positions and the remaining bits are independent and uniform. Since we have u = v + s, the *l* in the above theorem equals $u - \lambda = v + (s - \lambda)$ when B learns λ bits, i.e., $2^{v-l} = 2^{\lambda-s}$. This implies that for all $0 \le \lambda < s$ it holds that the probability that B is not caught and at the same time ΔA is not uniform is at most $2^{-\lambda}2^{\lambda-s} = 2^{-s}$. Clearly, for all $\lambda \geq s$, then the probability that B is not caught and at the same time ΔA is not uniform is at most the probability B is not caught, which is at most 2^{-s} . This shows that when u = v + s then for all B, the probability that B is not caught and at the same time ΔA is not uniform is at most 2^{-s} , which is negligible.

The consequence of our new analysis is that we can choose the random matrix as $A \in \{0, 1\}^{(v+s) \times v}$ and thus we only have to produce leaky Δ -ROTs of length v + s instead of length $^{22v/3}$, a substantial optimization. As we ultimately require (non-leaky) Δ -ROTs of length k, we can utilize any of the mentioned OT extension protocols to produce leaky Δ -ROTs of length k+s and then apply the linear randomness extraction on the resulting OT-strings. For the parameters s = 40 and k = 128 considered in this work our refined analysis ultimately yields an improvement of around a factor 5.6x compared to the previous best known result of [19].

IV. THE PROTOCOL

As already mentioned in Section I, our protocol is based on TinyLEGO [33], but modified to support preprocessing of all garbled components along with our new approach for dealing with the selective-OT attack of Section III-A. This includes removing the restriction of B choosing input and committing to the cut-and-choose challenges before obtaining the garbling material and solderings. As a consequence, our modifications allow for multi-leveled preprocessing and a very efficient online phase. We give a description of our resulting protocol in Fig. 1 and Fig. 2. See [33] for a more detailed specification of the original TinyLEGO protocol. At a high level our protocol can be broken down into four main steps.

- 1) The **Setup** phase initializes the commitment scheme. All public-key operations of our protocol can be carried out in this initial step, including the BaseOTs required for bootstrapping OT extension.
- 2) The Generate step takes as input the number of gates q, number of inputs n and number of outputs m the parties wish to preprocess. After sending the garbled gates and wire authenticators and committing to all associated wires, a cut-and-choose step is run between the parties. The wire authenticators is a gadget that either accepts or rejects a given key (without revealing the value of the key) and it was shown in [33] that constructing AND buckets from both garbled gates and wire authenticators can significantly reduce the overall communication compared to using garbled gates alone. After the cut-and-choose step, using the XOR-homomorphic commitments, the parties solder the remaining garbled gates and wire authenticators randomly into independent fault tolerant AND buckets.
- 3) The Build step takes as input the circuit description f and through the XOR-homomorphic commitments, A sends the required solderings to glue together a subset of previously produced AND buckets so that they compute f.
- 4) Finally, the Eval step depends on the parties' inputs to f. It consists of two rounds, first B sends a correction value e which depends on his input y, and as a response A decommits to B's masked input keys as well as sending it's own input keys directly. Finally A also decommitments to the lsb of all output 0-keys. This allows B to evaluate the garbled circuit and decode the final output.

We highlight that our modified protocol also naturally supports the notion of *streaming* or *pipelining* of garbled circuit evaluation [39] which was not the case in [33]. This can be seen by the fact that one can evaluate the circuit f in a layered approach and using the XOR-homomorphic commitments to glue the output of one layer onto the input of the next layer.

The Setup step is only required to be run once, regardless of the number of future calls to Generate. **Setup(pp):**

 On input (k, s, p_g, p_a, β, α, β, α) ← pp, A and B initialize the functionality F_{HCOM} by sending (init, sid, A, B, κ) to it, where κ is the key-length of the garbling scheme.

The Generate step produces q garbled AND gates which can be soldered into circuits that in total can have n inputs and m outputs. It is possible to do multiple calls to Generate at any point in time in order to produce more garbling material. **Generate**(q, n, m):

- 1) Let Q and A be chosen such that after running the below cutand-choose step, with overwhelming probability $(q\beta + n\tilde{\beta})$ garbled gates and $(q\alpha + n\tilde{\alpha})$ wire authenticators survive.
- A and B invoke F_{Δ-ROT} (n+s) times from which A learns Δ and random strings r_i⁰ and B learns the choice-bits b_i and r_i^{b_i} for i ∈ [n + s]. Furthermore, A instructs F_{Δ-ROT} to ensure that lsb(Δ) = 1.
- 3) Next, A garbles Q AND gates and constructs A wire authenticators using Δ and sends these to B.
- 4) A then commits to each wire of the garbled AND gates, each authenticated wire produced, Δ , the 0-strings received from $\mathcal{F}_{\Delta-\text{ROT}}$, and m+s random values $\{v_j\}_{[m+s]}$. Thus it sends 3Q + A + 1 + n + s + m + s values to $\mathcal{F}_{\text{HCOM}}$.

VerLeak:

- 5) For $i \in [n]$ and $j \in [m + s]$, A sends $lsb(r_i^0)$ and $lsb(v_j)$ to B.
- 6) B challenges A to send, using *F*_{HCOM}, *s* random linear combinations of r⁰_i, v_j and ∆ for *i* ∈ [*n*] and *j* ∈ [*m*]. Also, the *l*'th combination is set to include a one-time blinding value v_{m+l} for *l* ∈ [*s*].
- B verifies that lsb of the received s values correspond to the same linear combinations of the initial lsb values sent by A in step 5. In addition, if Δ is included in a linear combination B flips the value. This ensures that indeed lsb(Δ) = 1.

Cut-and-Choose:

- 8) After receiving the garbled gates (wire authenticators), B chooses to check any gate (wire authenticator) with probability p_g (p_a). B then challenges A to send, using $\mathcal{F}_{\text{HCOM}}$, two random inputs and the corresponding AND output of the selected garbled gates and a random input of the selected wire authenticators.
- 9) B evaluates the selected garbled gates and wire authenticators and checks that they output the received output key and that they verify the values received from \mathcal{F}_{HCOM} , respectively.
- 10) In addition, for $i \in [n; n+s]$ B sends $r_i^{b_i} = r_i^0 \oplus (b_i \cdot \Delta)$ to A which in turn instructs $\mathcal{F}_{\mathsf{HCOM}}$ to send back the same value. This is to ensure that the committed Δ is the one used in $\mathcal{F}_{\Delta-\mathsf{ROT}}$.

Bucketing:

- 11) For the remaining garbled gates (wire authenticators), B samples and sends a random permutation that fully describes how these are to be combined into q AND buckets of size $\beta + \alpha$, n input buckets of size $\tilde{\beta}$ and n input authenticators of size $\tilde{\alpha}$.
- 12) A then sends, using $\mathcal{F}_{\text{HCOM}}$, all the required solderings such that for all the specified bucket gadgets, each component is defined with the same input/output keys.

Fig. 1. The modified TinyLEGO protocol with support for preprocessing in the ($\mathcal{F}_{\text{HCOM}}$, $\mathcal{F}_{\Delta\text{-ROT}}$)-hybrid model (Part 1).

The Build step uses the garbling material created in Generate to construct a fault tolerant garbled circuit computing f. Build(f):

1) A instructs $\mathcal{F}_{\mathsf{HCOM}}$ to send the required solderings such that the first |f| unused AND buckets correctly compute f. This includes the solderings to attach n_{A} input buckets and ninput authenticators onto the final garbled circuit.

In the Eval step the parties transfer to B all input keys in an oblivious manner which then allows B to evaluate and decode the garbled circuit previously constructed using the Build step. **Eval**(x, y):

- 1) For input $y \in \{0, 1\}^{n_{\mathsf{B}}}$, B sends $e = b \oplus y$ to A, where b is the first n_{B} unused choice-bits of $\mathcal{F}_{\Delta-\mathsf{ROT}}$.
- A then instructs F_{HCOM} to send to the values {D_i = r_i⁰ ⊕ K_i⁰ ⊕ e_i · Δ}_{i∈[n_B]} where K_i⁰ is the 0-key on the *i*'th input wire of B and r_i⁰ is the first unused Δ-ROT string. Also, for the input x ∈ {0,1}^{n_A}, it sends the corresponding input keys {K_i^{x_i}}_{i∈[n_A]} directly to B.
- keys {K_i^x_i}_{i∈[n_A]} directly to B.
 3) Finally, A instructs *F*_{HCOM} to send the output decoding values {D_j = v_j⁰ ⊕ K_j⁰}_{j∈[m]} to B where K_j⁰ is the j'th output 0-key of the garbled circuit and {v_j}_{j∈[m]} are the first m unused blinding values setup in the VerLeak step.
- 4) Upon receiving the above, for i ∈ [n_B] B computes K_{n_A+i} = r_i^{b_i} ⊕ D_i and lsb(K_i⁰) = lsb(D_i) ⊕ lsb(r_i⁰) ⊕ e_i and verifies that lsb(K_{n_A+i}) ⊕ lsb(K_i⁰) = y_i. Then using the input authenticators, B also verifies that the keys {K_i}_{i∈[n_A]} of A are valid input keys to the garbled circuit.
- 5) If everything checks out, B evaluates the previously constructed garbled circuit on the input keys (K_1, K_2, \ldots, K_n) to obtain the output keys (Z_1, Z_2, \ldots, Z_m) . For $j \in [m]$ it then computes $d_j = \text{lsb}(v_j) \oplus \text{lsb}(D_j)$ and decodes $z_j = \text{lsb}(Z_j) \oplus d_j$. Finally, B outputs $z = (z_1, z_2, \ldots, z_m)$.

Fig. 2. The modified TinyLEGO protocol with support for preprocessing in the ($\mathcal{F}_{\text{HCOM}}$, $\mathcal{F}_{\Delta\text{-ROT}}$)-hybrid model (Part 2).

Each of these layers can be processed on the fly with our protocol and in this way the circuit never needs to be stored entirely at any given time. This approach is similar to that proposed in [59] for reusing garbled values, however in this setting everything works out-of-the-box due to the XOR-homormophic commitments on all circuit wires.

The LEGO approach also has the advantage compared to traditional cut-and-choose protocols that only a *single fault tol-erant* garbled circuit is produced and evaluated. This removes the necessity of ensuring input consistency for all the evaluation circuits. It also sidesteps the overhead of transferring multiple sets of input keys in the online phase, one set for each evaluation circuit.

A. Bucketing

With the bucketing approach of [33] each AND bucket consists of β garbled gates and α wire authenticators. For any garbled gate (wire authenticator) the probability p_g (p_a) is used to determine if it is checked in the cut-and-choose or not. The value of p_g and p_a therefore induces a certain sense of "quality" level of the remaining non-checked garbled components which affects the required bucketing size. In addition there are also the special cases of input buckets and input authenticators, which are buckets that consist of garbled gates only (size $\tilde{\beta}$) and wire authenticators only (size $\tilde{\alpha}$), respectively. These are attached to the input wires of the final garbled circuit and serve to guarantee validity of the input keys, along with guaranteeing that B can always learn the final output f(x, y), even if A is cheating. This is so since the input buckets can be seen as a trapdoor that together with the global difference Δ allows B to extract the input x of A. It is then clear that it can compute f(x, y) directly. These special buckets are necessary as our regular AND buckets do not rule out outputting both the 0 and 1-key (say if one of the garbled gates in the bucket is in fact a NAND gate). However, if a bucket outputs two distinct keys it is guaranteed that they are both valid and hence their XOR is Δ and B can extract x. If no cheating is detected then the input buckets are simply ignored by B.

As already established in the original LEGO paper [61], the number of AND gates q directly affects the required size of the buckets, meaning that as q grows the required bucket size can be decreased while still retaining the same level of security. Theorem 2 below gives a direct way of computing the success probability of a corrupt A given the parameters $q, n, \beta, \alpha, \tilde{\beta}, \tilde{\alpha}$.

Theorem 2 ([33], Lemma 9). Given the bucketing parameters $q, n, \beta, \alpha, \tilde{\beta}, \tilde{\alpha}$ for the case where $\alpha = \beta - 1$ we can bound the probability of the bad bucketing events occurring as:

$$\begin{aligned} &\Pr[\operatorname{Any \ bad \ bucket}] \leq \\ q \cdot \left(\quad \prod_{i=\beta}^{1} \quad \left(\frac{(1-p_g)4i}{p_g(q\beta+n\tilde{\beta})+(1-p_g)4i} \right) + \right. \\ & \left. \sum_{l=2}^{\beta} \quad \prod_{i=\beta}^{l} \left(\frac{(1-p_g)4i}{p_g(q\beta+n\tilde{\beta})+(1-p_g)4i} \right) \cdot \right. \\ & \left. \prod_{j=\alpha}^{\alpha+2-l} \left(\frac{(1-p_a)2j}{p_a(q\alpha+n\tilde{\alpha})+(1-p_a)2j} \right) \right) \end{aligned}$$

 $\Pr[\text{Any bad input authenticator}] \leq$

$$n \cdot \sum_{v=1}^{\lfloor \frac{\alpha}{2} \rfloor} \prod_{l=\tilde{\alpha}}^{v} \left(\frac{(1-p_a)2l}{p_a(q\alpha+n\tilde{\alpha})+(1-p_a)2l} \right)$$

 $\Pr[\text{Any bad input bucket}] \leq$

$$n \cdot \sum_{l=1}^{\left\lceil \frac{\beta}{2} \right\rceil} \prod_{i=\tilde{\beta}}^{l} \left(\frac{(1-p_g)4i}{p_g(q\beta+n\tilde{\beta})+(1-p_g)4i} \right)$$

Based on Theorem 2, given the number of AND gates qand the number of inputs n we directly compute the optimal choices of β , α , $\tilde{\beta}$, $\tilde{\alpha}$ for minimizing the overall communication of the protocol while still guaranteeing a negligible upper bound on the success probability of a corrupt A. This is a once and for all computation so for our implementation we have precomputed a table of secure choices using a simple script which is looked up on runtime when q and n have been decided. We note that it is also possible to minimize for lowest possible bucket size if desired. This has the effect of reducing the computational overhead in the online phase at the price of increasing both communication and computational overhead in the independent preprocessing phase. In our experiments in Section VI we solely minimize for overall communication.

B. Security

Our protocol is similar to the TinyLEGO protocol in [33] and the proof follows the same general outline. We will therefore only give a very brief sketch of the overall proof strategy and then describe how to deal with the changes we made relative to TinyLEGO.

Consider first the case where the garbler A is corrupted. As is typically the case it is easy to see that the communication of the protocol does not leak any information on the input of B as long as the protocol does not abort. The garbler A might however give wrong input to some of the OTs used by B to choose its input keys, giving rise to selective errors where the abort probability depends on the input of B. The garbler A might also create some bad garbled gates which could a priori result in an abort or a wrong output, which might both leak information on the input of B. The problem with bad gates is handled exactly as in [33], by setting the cut-and-choose parameters and bucket sizes appropriately. We however handle the case with bad inputs to the OTs differently, as described below. In the universal composability (UC) framework [20], when A is corrupt, we also need to be able to extract the input of the corrupted A from its communication and input to ideal functionalities (OT and commitment). We handle this exactly as [33]: the cut-and-choose ensures that most key authenticators only accept their two corresponding committed keys. For a good key authenticator the accepted key can then be compared to the committed values to compute its semantic value. The bucket size has been set such that there is a majority of good key authenticators on all input wires. This allows to compute the semantic of any accepted key by taking majority.

Consider then the case where the evaluator B is corrupted. As is typically the case, the communication clearly does not leak information to B about the input of A. All that is left is therefore to describe how to handle two technical requirements imposed by the UC framework. First, we have to describe how to extract the input y of a corrupted B. Second, after learning yand z = f(x, y) we must enforce that the simulated protocol constructs a circuit that evaluates to z. This must be done without knowing x. Extracting y is handled exactly as in [33]. We simply inspect which choice bits B uses in the OTs for selecting its input. Hitting z in the simulation is also handled exactly as in [33]. We simply construct the circuit correctly and run with input 0 for A. This gives a potentially wrong output z' = f(0, y). We patch this by giving appropriately chosen wrong output decoding information by opening a wrong least significant bit of the output key for the output wires *i* where $z'_i \neq z_i$. This is possible as the simulator controls the ideal functionality for commitment in the simulation.

We now focus on the changes we made to [33].

Change 1 In both protocols the output decoding information consists of the least significant bit of the output keys, securely leaked via the commitment scheme. However, the implementation differs. We use a noninteractive implementation which is slightly heavier on communication. In [33] they use an interactive protocol with less communication.

- Change 2 In [33] they let B commit to the cut-and-choose challenges and choose his input via OT before obtaining the garbled gates, wire authenticators and solderings. We have removed this step. Now B picks his input after the circuit is constructed and does not commit to his challenges.
- Change 3 In our protocol we take the global Δ -value output by the OT extension and reuse it as the global Δ in the Free-XOR garbling scheme. In [33] they use two independent values.
- Change 4 We protect against selective error on the input of B by using the same Δ in OT extension and garbling and using a Δ -ROT to offer the input keys to B. We also leak the least significant bit of the Δ -OT 0strings to B for all his input wires. In [33] a different technique was used.

Change 1 does not affect security. It was introduced to give better execution time for typical circuits.

We now address Change 2. The reason why B commits to the cut-and-choose challenges and chooses his input via OT before obtaining the garbled material in [33] is that security is proven via a reduction to a standard (non-adaptive) selective garbling scheme (e.g. [12]), where the adversary in the security game must supply its input before it gets the garbled circuit. Therefore they need to be able to extract the input and cut-andchoose challenges of B before assembling the garbled circuit in the simulation. We have skipped this step as it would prevent independent preprocessing. Now that we assemble the circuit before B picks its input, the hope would be that we could do a reduction to an adaptive garbling scheme. However, due to the soldering approach of LEGO where the XOR of 0keys are sent to the evaluator before the input is determined, it is unclear how to reduce security to the standard notion of adaptive garbling, as some of these 0-keys are not known to the simulator. To overcome this we instead identify the defining property we need from the underlying garbling function which is that the outputs of the hash function appear random as long as the inputs are all unknown and have sufficient entropy, even if the inputs are related. A non-extractable, non-programmable random oracle clearly satisfies this property [13]. The type of garbling scheme considered in this work [72] could in principle be made adaptively secure by using a programmable random oracle using techniques described in [11], [55].¹ We avoid using the programability of the random oracle by changing the usual approach a little. Normally security proofs need to program the circuit to hit the right output. We instead garble the circuits correctly and then program or equivocate the output decoding information to decode to the value we need to hit. Specifically we use equivocation of the UC commitment scheme to incorrectly open the least significant bit of the output keys when we need to hit a different value. Returning to the simulation, we therefore garble all gates and answer all cutand-choose challenges honestly. As we now know all garbling keys we can also open consistently to differences between 0keys for the remaining evaluation gates. Finally, in order to

¹It is also possible to build an adaptively secure garbling scheme (with short input keys) using a non-programmable random oracle [9], but this particular scheme is not as efficient as the one of [72].

make the complete soldered garbled circuit "hit" the output z we equivocate the openings of the least significant bits of the output keys such that this becomes the decoded value. This is possible as the decoding information is only opened after we extract the input of the corrupt receiver. If the garbling is done using a random oracle this will have the same distribution as in the protocol.

For Change 3 we again use that we are in the random oracle model. The first step in the proof will be to go from the case where Δ is reused in the garbling scheme to the case where an independent Δ' is used for garbling as in [33]. In this hybrid we also let A commit to Δ' . We then use equivocation of the commitment scheme to make the cut-and-choose proof that $\Delta' = \Delta$ go through. Since B only sees one key for each wire and has high entropy on Δ and Δ' , this change will be indistinguishable to B if the output of the hash function appears random as long as the inputs are all unknown and have sufficient entropy, even if inputs are related. As above, a non-extractable, non-programmable random oracle clearly satisfies this property.

We finally address Change 4. Using a Δ -ROT to offer the input keys to B ensures that when A inputs the keys to the OT, either both are correct or both are incorrect. If both are incorrect, it will be detected by a key authenticator independently of the input of B. This means that the only remaining attack vector is for A to swap the two correct keys. This is detected by B as B knows the least significant bit of the Δ -ROT 0-strings and the two correct keys have different least significant bits. Again the detection is independent of the input of B. Notice that the output decoding information is sent to B using $\mathcal{F}_{\text{HCOM}}$ after he sends his input correction value *e*, so we can equivocate it to hit the correct output *z*. This, together with the fact that the outputs of the hash function appear random, is why it is secure to perform the VerLeak step before learning the input of B.

As argued above, our modified protocol can be proven secure in the non-extractable, non-programmable random oracle model following the proof of [33]. As we do not require programmability of the random oracle we conjecture that our protocol can be proven secure in the standard (OT hybrid) model using the recently proposed ICE framework of [31], an extension of the UCE framework of [9]. However, we note that it does not seem like our scheme can be proven secure using the UCE framework as in our setting all the garbled gates are related (all garbled with the same Δ) and therefore a single leakage phase as prescribed in the UCE framework seems insufficient.

V. IMPLEMENTATION

In this section we highlight some of the more technical details of our implementations of the XOR-homomorphic commitment scheme and our final 2PC protocol supporting independent preprocessing. The source code of the project can be found at https://github.com/AarhusCrypto/TinyLEGO.

A. UC-Secure XOR-Homomorphic Commitments

As part of our full 2PC prototype we implement the XOR-homomorphic commitment scheme of [34] as a separate subprotocol. This is to our knowledge the first time a scheme

following this OT + PRG blueprint has been implemented and we believe our experimental findings are of independent interest. At a high level, the scheme works by the parties initially doing \tilde{n} BaseOTs of security parameter k-bit strings, where \tilde{n} is the code-length for some linear error correcting code C with parameters $[\tilde{n}, \kappa, s]_{\mathbb{F}_2}$ with κ being the bitlength of the committed messages. The parties then expand the received k-bit strings into bit-strings of length γ using a PRG which then define the γ random commitments the sender is committing to. Next, the sender sends a correctional value for each produced commitment to turn these into codewords of C. Finally, to ensure that the sender sent valid corrections, the receiver challenges the sender to decommit to 2s random linear combinations of all produced commitments. This is done in a way such that no information is leaked about the γ committed values. Additively homomorphism then follows from the fact that the code C is linear and all operations on the expanded PRG strings are linear as well. We highlight the fact that any XOR homomorphic commitment scheme supports the notion of batch opening/decommitment which is similar in nature to the above consistency check. The idea is that the sender initially sends the decommited values directly to the receiver, who hereafter challenges the sender to decommit to s linear combinations of the postulated values where s is the statistical security parameter. Notice that it is only in the initial commit step that 2s combinations are necessary. If the decommitted values match the linear combinations of the postulated values, the receiver accepts. As now only s values are decommitted this approach has the benefit of making the communication overhead independent of the number of values decommitted to. For the full details we refer to [34].

We implement the above scheme in C++14 taking advantage of multi-core capabilities and Intel SSE instructions. We can therefore base the PRG on AES-NI in counter mode and for the error correcting code we use a modified version of the linux kernel implementation of the BCH code family [17], [38]. As part of the commitment step the parties are required to transpose a binary matrix $S \in \{0, 1\}^{\bar{n} \times \gamma}$ in order to efficiently address the committed values in column-major order. As γ in our case can be huge (> 220 Mio. for 2000 AES-128 computations) we use the efficient implementation of Ekhlund's cache-efficient algorithm for binary matrix transposition [30] presented in [5], [6].² As a side note we also augment the OT extension code to support the randomness extraction technique described in Section III-A to implement the $\mathcal{F}_{\Delta-\text{ROT}}$ functionality needed in our 2PC protocol.

During the development of our implementation we identified the main computational bottleneck of the scheme to be the computation of the random linear combinations. Even if these operations are based on mere XORs, when implemented naively, the number of required instructions is still γs in expectation. Therefore, inspired by [21], we use a different approach for computing the consistency checks using Galois field multiplication. Combined with efficient matrix transposition the effect of using $GF(2^l)$ multiplication can be seen as computing *l* linear combinations in parallel. For our particular setting we set l = 128 as this is the smallest power of 2 greater than the required 2s for s = 40. We can then use the Intel SSE instruction PCLMULQDQ to very efficiently

²Available at https://github.com/encryptogroup/OTExtension

γ	#Threads	Co	mmit [µs]	Decommit [µs]
500	1	7.21	(2815.28)	2.20
1000	2	3.85	(1401.83)	1.40
15000	4	0.64	(93.99)	0.34
50000	8	0.57	(28.49)	0.22
500000	20	0.45	(3.25)	0.17
10000000	200	0.21	(0.35)	0.14
200000000	400	0.20	(0.21)	0.14

TABLE III Timings for committing to γ strings of length 128 BIT WITH s = 40. All timings are μ s per commitment. The commit TIME IN PARENTHESES INCLUDES THE COST OF THE INITIAL BASEOTS.

compute the $GF(2^{128})$ multiplications. In detail, our approach to compute the checks is as follows:

- 1) Given a random challenge element $\alpha \in_R GF(2^l)$ the matrix S of committed values in column-major order is split into $u = \lceil S/l \rceil$ blocks $B_i \in \{0, 1\}^{\tilde{n} \times l}$. Each block is then transposed into row-major order.
- 2) For $i \in [u]$ and $j \in [\tilde{n}]$, the new matrix $B'_i = B^j_i \cdot \alpha^i$ 2) For i ∈ [u] and j ∈ [u], the new many -i is computed where B^j_i ∈ {0,1}^l is the j'th row of B_i interpreted as an element of GF(2^l).
 3) Finally, the combined matrix B' = ∑^u_{i=1} B'_i is produced
- and transposed back into column-major order.

Each column of B' can now be seen as a random linear combination of all values of S. As a further optimization we see that most GF elements are only multiplied a single time in the above and we can therefore postpone the expensive degree reduction step of the multiplication until B' has been fully computed. This is different for computing α^i which we therefore reduce at each iteration. In total the required number of degree reductions becomes n+u as opposed to (n+1)u. Our experiments show that using the above method of computing 128 linear combinations compared to the naive approach is between 10-13x faster starting at a moderate number of random commitments $\gamma > 8000$.

As our implementation of the XOR-homomorphic commitment scheme might be of independent interest we here present our observed timings for committing and decommitting to γ random bit-strings of length 128 with k = 128 and s = 40. We instantiate the binary BCH code with parameters [312, 128, 41] and for convenience we use the implementation of [6] augmented with our randomness extraction technique to compute the required 312 Random OTs. In total this takes about $1400 \,\mathrm{ms}$ with our implementation, where $1392 \,\mathrm{ms}$ are due to the BaseOTs (using PVW [63]). From the timings reported in [23] we predict that this initial setup step can be done much faster (around 20 ms) using their implementation, but since this requires a programmable random oracle assumption and this cost amortizes away as γ grows we did not pursue this. Also, if the commitment scheme is used in an application that already relies on oblivious transfer, OT extension can be used to produce the starting BaseOTs at very low cost. We report our findings in Table III. As the scheme requires \tilde{n} BaseOTs to setup we include this cost in the commit timings in parentheses. It can thus be seen by comparing the commitment numbers how the initial OT cost amortizes away as γ increases. As there is no initial cost associated with decommitment these timings are only affected by the number of worker-threads we spawn. Furthermore, these experiments were performed on the local LAN setup described in Section VI and *not* on the Amazon Web Services (AWS) architecture.

B. 2PC with preprocessing using LEGO

We implement the TinyLEGO protocol with our modifications on top of the previously described commitment scheme. The code is also written in C++14 and makes heavy use of parallelism and Intel SSE instructions for garbling and evaluation of the garbled gates. At a high level, the Generate step is implemented by first partitioning the inputs (q, n, m)into t equally sized subsets for some parameter t. The main thread then starts t parallel executions of the generate step with two synchronization points, one where the commitment to Δ is sent (which only one execution is charged with), and one after the cut-and-choose step. The latter is necessary as the random permutation that describes the initial bucketing must only be revealed after all garbled components have been sent to B. We emphasize that it is due to our preprocessing being independent of the structure of f that we can trivially parallelize the above step using any number of threads t. Due to the above design we also run t executions of the commitment scheme, however for the PRG expansion we use the same seed OT values in all executions. As the PRG is based on a block cipher in counter mode this is not an issue as execution i + 1 sets it's counter sufficiently high compared to the *i*'th execution so there is no overlap. Since they all use the same seed OTs the choice-bits are also the same across all executions and they can therefore be combined in the same way as for a single execution.

The Build and Eval phases follow roughly the same design pattern as above. We note however that in these phases each thread is responsible for soldering and evaluating an entire circuit. The garbling and evaluation of garbled gates and wire authenticators are implemented purely as 128-bit SSE instructions to maximize performance. We base the hash function for garbling gates and producing wire authenticators on Fixed-Key AES-NI as advocated in [10]. This choice is mainly motivated by producing as comparable results as possible to previous works that are also based on Fixed-Key AES-NI.

The Eval phase consists of two rounds, one where B specifies the input mask and one where A replies with its keys and decommitments. A's reply has communication complexity kn_A for A's input keys and $(\tilde{n} + k)(n_B + m)$ for the decommitments of B's input keys and the lsb masks of the output keys, where \tilde{n} is the code-length of the BCH code. We note that the communication cost of the decommitments can be reduced to $(\tilde{n} + k)s + k(n_{\mathsf{B}} + m)$ using the batch decommit approach mentioned in Section V-A, but at the cost of adding an additional round. For the circuits used in our experiments (AES-128, SHA-256) we observed a loss of around a factor 1.25 in the LAN setting and much more in the WAN setting with this approach. Still, for other circuits where the ratio $(n_{\rm B}+m)/|f|$ is substantial and both network latency and bandwidth are low we suspect that adding this extra round can pay off. Finally if one is willing to assume a programmable random oracle the online cost for the output bits can be eliminated entirely as the simulator then can program the oracle to output matching output keys for a preprocessed decommitment lsb-bit once it learns the final output.

VI. PERFORMANCE

To give a broad view of the performance of our prototype we run experiments in a local LAN setting and on both a LAN and WAN on the Amazon Web Services (AWS). In more detail:

- Local LAN with two machines, one acting as A and the other acting as B. We measured a total bandwidth of 942 Mbits/sec with round trip time (rtt) 0.12 ms. Both machines run Ubuntu 16.04 with an Intel Ivy Bridge i7 3.5 GHz quad-core processor and 32 GB DDR3 RAM.
- **AWS LAN** with two c4.8xlarge instances located in the Virginia region connected via a high performance LAN. We measured a bandwidth of 9.52 Gbits/sec with rtt 0.16 ms. Both machines run Amazon Linux AMI 2016.03.2 with an Intel Xeon E5-2666 v3 (Haswell) processor with 36 vCPUs and 60 GB RAM.
- **AWS WAN** with two c4.8xlarge instances, one in Virginia and one in Ireland. We measured a bandwidth of 214 Mbits/sec on average for a single TCP connection and up to 3.17 Gbit/sec when running many parallel connections. The rtt measured was 81.32 ms. Both machines run Amazon Linux AMI 2016.03.2 with an Intel Xeon E5-2666 v3 (Haswell) processor with 36 vCPUs and 60 GB RAM.

For all settings the code was compiled using GCC-5.4 with the -O3 optimization flag set. As mentioned in Section V-A the implementation used for the BaseOTs are based on [6] using PVW [63]. If one is willing to assume a programmable random oracle, these can be replaced with the fast protocol and implementation of [23] and we would expect a total cost around 20 ms as opposed to 850 ms (AWS LAN) with the current implementation.

A. Our Performance Results

We summarize our measured results in Table IV on the following page for the three above-mentioned settings. All numbers reported are averages of 10 executions. Not surprisingly we see the best performance on the AWS machines in the LAN setting where we can evaluate an AES-128 circuit with latency 1.13 ms or 0.08 ms throughput per AES-128 in the online phase. We also see that when considering 1024 AES-128 evaluations the dependent preprocessing + the online phase is below 2 ms. When including the cost of the independent preprocessing each AES-128 can be done in total time less than 16 ms. Similarly when considering 256 SHA-256 evaluations the online phase can be done with latency $9.14 \,\mathrm{ms}$ or $1.05 \,\mathrm{ms}$ of throughput per SHA-256. Also the dependent preprocessing + online phase and total cost is below $22 \,\mathrm{ms}$ and $205 \,\mathrm{ms}$, respectively (when preprocessing material enough for 256 SHA-256 evaluations).

For the single execution setting we see a significant increase in execution time for the dependent preprocessing compared to above. This is due to the design of our prototype which only uses multiple execution threads in the dependent preprocessing and online phases if several, possibly different, circuits are processed at the same time. We also note that our prototype requires a large amount of RAM as we store all garbling material and commitments in-memory. This design choice is due to convenience, but for a deployed system based on the LEGO approach this should be addressed using external memory sources with support for pipelined evaluation as described in Section IV.

For the AWS WAN setting we see that a single execution of AES-128 takes around 83 ms online time where almost all of the runtime is spent waiting due to a latency of ~ 81 ms. The latency also severely impacts the two preprocessing phases where the independent preprocessing takes around 1882 ms (20x compared to AWS LAN) and the dependent offline phase takes 96 ms (7x compared to AWS LAN). However this overhead can be somewhat mitigated when considering several circuits, down to a factor 2-4x compared to AWS LAN due to the computation and communication being more interleaved and better utilization of the bandwidth with several TCP connections.

Finally in Table V on the next page we report on the amount of data our prototype transfers from the circuit constructor to the circuit evaluator for both AES-128 and SHA-256. For clarity we have not included the communication from evaluator to constructor, but note that for 1024 AES-128 and 256 SHA-256 a total of $8.12\,\mathrm{MB}$ and $4.09\,\mathrm{MB}$ are transferred, respectively, and for both cases around 99% of the communication stems from the initial BaseOTs. The table also summarizes the bucketing parameters used in our experiments, which have been chosen so that the probability bound given by Theorem 2 in Section IV-A is negligible. Also we set the two input bucket parameters $\hat{\beta} = 2\beta + 1$ and $\tilde{\alpha} = 2\alpha + 1$ which ensures a correct majority for all the input buckets and authenticators except with negligible probability. For the data numbers in Table V it can be seen in parentheses how the relative preprocessing cost of a circuit decreases as more evaluations are considered. We highlight that in this work (and previous LEGO protocols) this is due to the increasing number of gates produced, not by the number of circuits. As an example of this effect, going from a single AES-128 with 6928 gates³ to 1024 AES-128 with 7094272 gates decreases the cost of the independent preprocessing by a factor 2.3x per AES-128, from 14.94 MB to 6.42 MB. It is worth noting that the "LEGO effect" only applies to the independent preprocessing. This is because in the subsequent dependent preprocessing step two solderings (k bits each) are sent per gate of the circuit f and not for each garbled gate produced. In addition a small constant 2.2 kB of decommitment data is transferred in this phase for the *s* challenge linear combinations. For the online step the communication consists of $n_A k$ bits for the constructors input + $(\tilde{n} + k)(n_B + m)$ bits for the decommitments to the evaluators input and the output decoding bits where \tilde{n} is the code-length of the ECC C used in the commitment scheme. In Section V-B we discussed how this could further be reduced to $(\tilde{n} + k)s + k(n_{\mathsf{B}} + m)$ at the price of adding an extra round to the online phase.

B. Comparison with Related Work

We compare our measured timings to those reported in the recent works of [56] and [65], both of which are solely applicable in the amortized setting. In contrast our protocol can naturally handle the single execution setting, along with a more general amortized setting where several *distinct* functions

³We use the AES non-expanded circuit of [68] which has 6800 AND gates. However we augment the circuit with identity gates on the 128 output wires in order to simplify output decoding using VerLeak.

Setting	Circuit	Number	BaseOTs	Ind. Preprocessing	Dep. Preprocessing	Online (latency)	Online (throughput)
Local LAN	AES-128	1 32 128 1024	1400.89 44.90 11.23 1.40	220.44 87.63 70.89 61.33	15.12 3.35 2.95 2.85	2.52 2.25 1.86 1.60	2.52 0.35 0.26 0.25
	SHA-256	1 32 128	1400.39 44.94 11.22	1381.05 812.12 771.27	208.00 44.59 37.72	22.65 11.77 10.43	22.65 3.12 3.02
AWS LAN	AES-128	1 32 128 1024	850.42 26.61 6.65 0.84	89.61 27.91 14.85 13.84	13.23 0.85 0.68 0.74	1.46 1.23 1.15 1.13	1.46 0.18 0.09 0.08
AWS LAW	SHA-256	1 32 128 256	852.90 26.82 6.67 3.34	478.54 165.26 173.05 183.51	164.40 14.87 12.13 11.70	11.19 9.14 9.35 9.56	11.19 1.42 1.09 1.05
AWS WAN	AES-128	1 32 128 1024	2980.25 93.75 23.44 2.96	1881.63 142.00 72.31 39.18	96.66 5.19 3.96 2.12	83.17 83.21 83.65 83.15	83.17 2.71 0.73 0.62
AWS WAN	SHA-256	1 32 128 256	3043.64 92.98 23.66 11.75	2738.62 670.98 431.71 356.48	350.01 42.01 25.44 27.97	93.94 92.42 92.38 92.74	93.94 4.04 1.70 1.87

TABLE IV. EVALUATOR TIMINGS MEASURED IN THE LOCAL LAN, AWS LAN AND AWS WAN SETTING FOR AES-128 and SHA-256 with k = 128AND s = 40. All timings are ms per circuit.

Circuit	Number	β	p_g	α	p_a	Base	OTs	Ind. Prep	processing	Dep. Prej	processing	On	line
	1	7	2^{-4}	6	2^{-3}	$19.52\mathrm{kB}$		14.94 MB		226.86 kB		16.13 kB	
AFS-128	32	4	2^{-2}	3	2^{-2}	$19.52\mathrm{kB}$	(610 B)	$279.78\mathrm{MB}$	$(8.74 \mathrm{MB})$	7.26 MB	(226.86 kB)	516.10 kB	(16.13 kB)
71L5-120	128	4	2^{-3}	3	2^{-3}	$19.52\mathrm{kB}$	$(153 \mathrm{B})$	$924.68\mathrm{MB}$	$(7.22 \mathrm{MB})$	$29.04\mathrm{MB}$	(226.86 kB)	$2.06\mathrm{MB}$	(16.13 kB)
	1024	4	2^{-5}	3	2^{-6}	$19.52\mathrm{kB}$	(19B)	$6.57\mathrm{GB}$	$(6.42\mathrm{MB})$	$232.31\mathrm{MB}$	$(226.86\mathrm{kB})$	$16.52\mathrm{MB}$	$(16.13 \mathrm{kB})$
	1	5	2^{-3}	4	2^{-4}	$19.52\mathrm{kB}$		120.34 MB		2.93 MB		$22.23\mathrm{kB}$	
SHA-256	32	4	2^{-4}	3	2^{-5}	$19.52\mathrm{kB}$	(610 B)	$2.73\mathrm{GB}$	$(85.19{\rm MB})$	93.63 MB	(2.93 MB)	712.70 kB	(22.23 kB)
5111-250	128	4	2^{-6}	3	2^{-5}	$19.52\mathrm{kB}$	$(153 \mathrm{B})$	$10.31\mathrm{GB}$	$(80.54\mathrm{MB})$	$374.52\mathrm{MB}$	$(2.93 \mathrm{MB})$	$2.85\mathrm{MB}$	(22.23 kB)
	256	4	2^{-7}	3	2^{-5}	$19.52\mathrm{kB}$	$(76 \mathrm{B})$	$20.28\mathrm{GB}$	$(79.20\mathrm{MB})$	749.03 MB	$(2.93\mathrm{MB})$	$5.70\mathrm{MB}$	$\left(22.23kB\right)$

TABLE V.Bucketing parameters and data received by the evaluator in the different phases of our protocol for AES-128 and
SHA-256 with k = 128 and s = 40. Numbers in parentheses are data per circuit produced.

Protocol	Setting	Number	Ind. Preprocessing	Offline	Online
[56]	AWS LAN	32 128 1024	× × ×	197 114 74	12 10 7
	AWS WAN	32 128 1024	× × ×	1126 919 759	163 164 160
[65]	AWS LAN	32 128 1024	× × ×	45 16 5.1	1.7 1.5 1.3
	AWS WAN	32 128 1024	× × ×	282 71 34	190 191 189
This Work	AWS LAN	32 128 1024	54.52 21.5 14.68	0.85 0.68 0.74	1.23 1.15 1.13
	AWS WAN	32 128 1024	235.75 95.75 42.14	5.19 3.96 2.12	83.21 83.65 83.15

TABLE VI. COMPARISON OF THE REPORTED TIMINGS FOR AES-128 IN THE AWS LAN AND AWS WAN SETTING WITH k = 128 and s = 40. The preprocessing column includes the cost of the BaseOTs FOR THIS WORK. All TIMINGS ARE mS PER AES-128. BEST RESULTS MARKED IN BOLD.

can be preprocessed in the same batch. However to make a meaningful comparison we focus on the "traditional" amortized setting considering 32, 128, and 1024 AES-128 computations and we summarize the comparison in Table VI. The independent preprocessing timings for our protocol consists of the BaseOTs + the independent preprocessing. The first thing to notice is that for applications where independent preprocessing is applicable, and can therefore be disregarded, our dependent offline performance is superior to both prior works for any number of AES-128 computations by a large margin. Compared to [56] our reported timings are better by 100-358x depending on the setting and number of circuits. For [65] the gap is smaller, but still substantial, namely by 6-54x. For applications where independent preprocessing can not be utilized we are still superior to the work of [56], but for most settings and number of circuits we cannot compete with the offline phase of [65]. However the differences are typically within a factor 1.2-3x.

For the online timings in the AWS LAN setting for AES-128 we measure faster overall timings than [65] for all number of circuits by a tiny margin. As the differences are less than half a millisecond we believe the only reasonable thing to conclude is that the online times are comparable. Though

Protocol	Number	Ind. Preprocessing	Offline	Online
[56]	32 128 1024	× × ×	$\begin{array}{c} 8.13{\rm MB} \\ 5.45{\rm MB} \\ 3.76{\rm MB} \end{array}$	312 kB 238 kB 170 kB
[65]*	32 128 1024	× × ×	$3.75{ m MB}\ 2.5{ m MB}\ 1.56{ m MB}$	$25.76{ m kB}\ 21.31{ m kB}\ 16.95{ m kB}$
This Work	32 128 1024	$\begin{array}{c} 8.74{\rm MB} \\ 7.22{\rm MB} \\ 6.42{\rm MB} \end{array}$	226.86 kB 226.86 kB 226.86 kB	16.13 kB 16.13 kB 16.13 kB

TABLE VII. Comparison of the data received by the evaluator for different number of executions of AES-128 with k = 128 and s = 40. All numbers are data per AES-128. Best results marked in bold.

when looking at raw throughput we outperform [65] by more than a factor 3x (0.08 ms vs, 0.26 ms). Going beyond Table VI and considering the larger SHA-256 circuit we note that our online phase is not faster than [65] (9.35 ms vs. 8.8 ms for 128 circuits). This is again due to the design of our prototype that uses a single execution thread in the online phase per circuit, while [65] uses several threads. We therefore see it as an interesting problem for future research to tailor the LEGO online phase to better exploit parallelism for a single circuit.

With regards to online latency in the AWS WAN setting there is however no doubt that our two round online phase outperforms both [56] and [65]. This is directly related to the previous protocols having more rounds which in a high latency network significantly decreases performance. For comparison [56] has a 4 round online phase and [65] has 5. One thing to note however is that [65] delivers output to both parties in 5 rounds, whereas both our work and [56] would need an extra round to support this. Also the implementation of [56] is written in a mix of Java and C++ using JNI which definitely adds overhead to the running time. It is however unclear how much of a speedup a native implementation would achieve, but we suspect it would be substantial. The implementation of [65] is written solely in C++ and according to the paper also takes full advantage of parallelization.

In Table VII we summarize the required communication for the previously considered protocols and our work for the same setting as Table VI. As was the case for the measured timings, when disregarding the cost of the independent preprocessing, our protocol requires significantly less communication in both the offline and online phase compared to the previous works. For the offline phase the communication is 5-12x less than [65] and 16-358x less than [56]. If the independent preprocessing is included as part of the offline phase our protocol however requires transferring more raw data than the previous two works for any of the considered number of circuits. However this is only so because we are considering multiple copies (32, 128, and 1024) of the same function AES-128. If we instead consider settings with few copies (the larger the better), a single copy, or several different circuits, the amount of data received in the independent + dependent preprocessing phase of our protocol can match or be lower than the dependent offline phase of [65], depending on the circuit sizes and number of circuits considered. Also, as [65] uses the dual-execution paradigm where both parties send and receive the same amount of data, the above comparison is only meaningful assuming a full-duplex channel which might not always be available. Finally, even if the amount of data received by the evaluator in our protocol is up to $\sim 4x$ that of [65] in Table VII, due to the highly parallelizable nature of our independent preprocessing phase, this does not translate into equivalently lower performance as can be seen in Table VI.

For the online phase, our protocol is more data-efficient than the previous works for any of the considered settings. In particular, we require sending 16.13 kB per AES which is around 1.05-1.6x less data than [65] and 10.5-19x less than [56], depending on the number of executions considered. Furthermore if one is willing to assume a programmable random oracle, as is already the case of both [65] and [56], our online phase can easily be modified to only sending 6.30 kB (using 3 rounds) or 9.09 kB (using 2 rounds) as explained in Section V-B.

Finally as mentioned in Section I and summarized in Table I the best reported timings for evaluating a single AES-128 is $65 \,\mathrm{ms}$ in [69]. Based on the reported numbers in their paper we estimate that $\sim 20 \,\mathrm{ms}$ of the execution time consists of the initial BaseOTs. We therefore consider the actual cost of their protocol to be around 45 ms and motivate this by observing that a single computation of BaseOTs can be reused for any number of future executions using OT extension. To give as meaningful a comparison as possible we also ran our implementation on the same AWS setup (c4.2x instance) for the single execution AES-128 case measuring 105.7 ms of ind. preprocessing time, 12.07 ms dep. preprocessing time and 1.41 ms online time on a LAN. Therefore our protocol performs around 2.5x times slower than theirs in total time (when also ignoring the cost of our initial BaseOTs). However if ind. preprocessing can be applied, then from the time the circuit is input by the parties, our protocol takes around 13.48 ms to evaluate, which is around 3.5x faster than [69]. We ran the same experiment in the WAN setting where we evaluate an AES-128 in 1837 ms of ind. preprocessing time, $82.51 \mathrm{ms}$ dep. preprocessing time and $72.63 \mathrm{ms}$ online time. As [69] takes 1513 ms in total, when adjusting for initial BaseOT cost the difference is about a factor 1.5x in favor of the latter. However, when ignoring time for independent preprocessing our protocol can perform around an order of magnitude faster. We believe this difference in factors between LAN and WAN is due to our protocol having fewer rounds (when ignoring our preprocessing) and our implementation fully saturating the network as it sets up multiple parallel TCP connections for maximal bandwidth utilization.

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