



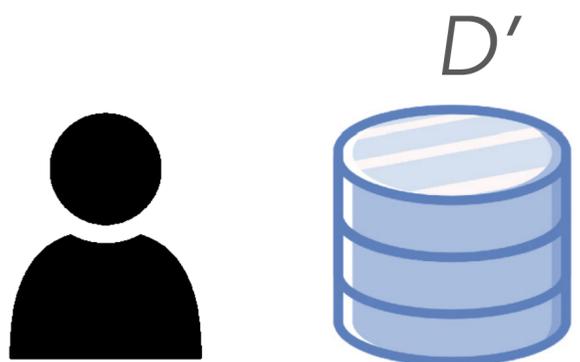
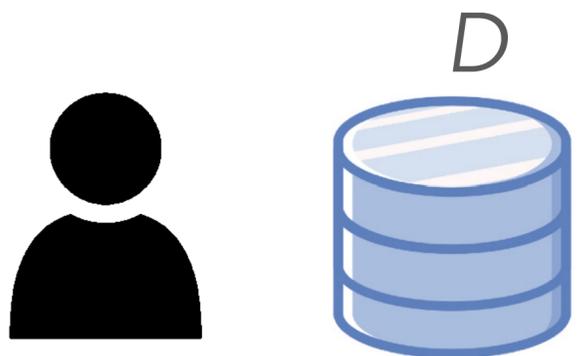
# To Shuffle or not to Shuffle: Auditing DP-SGD with Shuffling

Meenatchi Sundaram Muthu Selva Annamalai, Borja Balle,  
Jamie Hayes, and Emiliano De Cristofaro

# Differential Privacy

# Differential Privacy

Neighboring  
Datasets

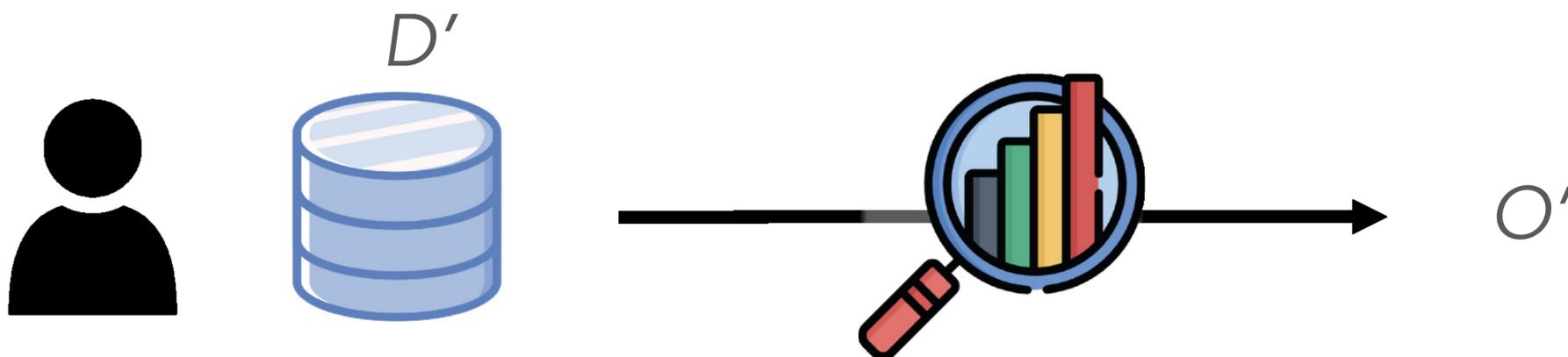
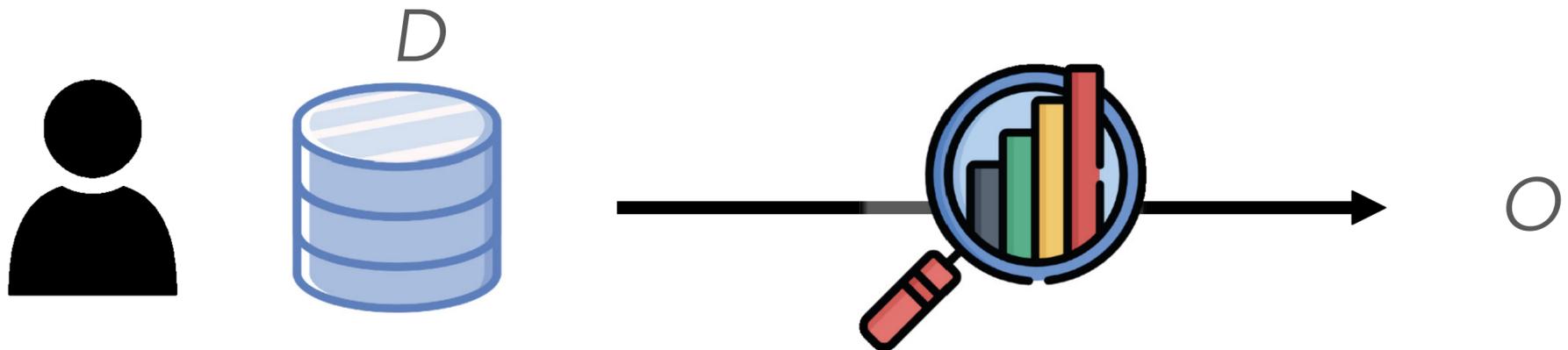


# Differential Privacy

Neighboring  
Datasets

Algorithm

Output



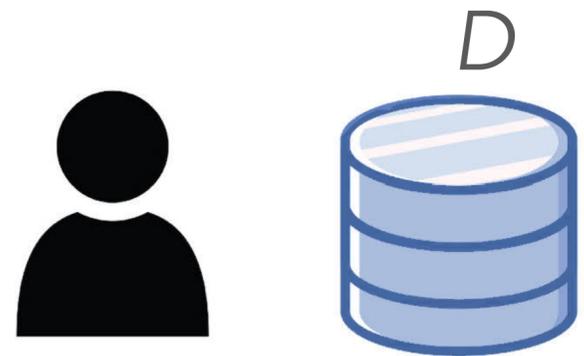
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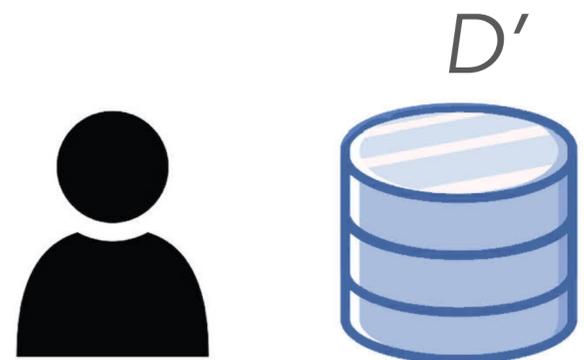
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$O$



$O'$

$O$  and  $O'$  are roughly similar  
(can't distinguish between them)  
for any  $D, D'$

With probability bounded  
by privacy parameter  $\epsilon$

# DP-SGD

1 iteration

Dataset

$x_1$

$x_2$

...

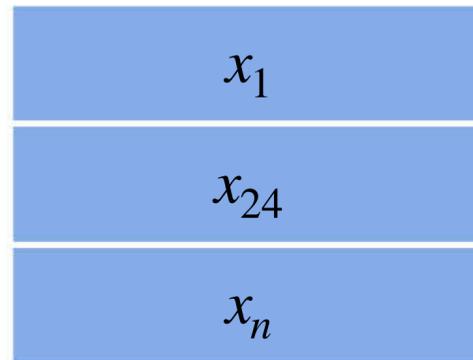
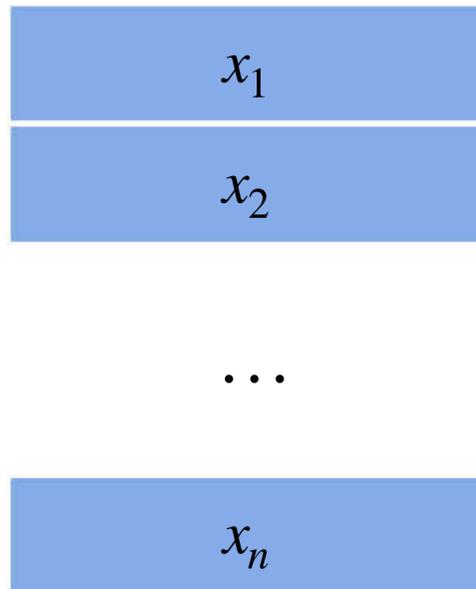
$x_n$

# DP-SGD

1 iteration

Dataset

Batch



**Sub-sampling**

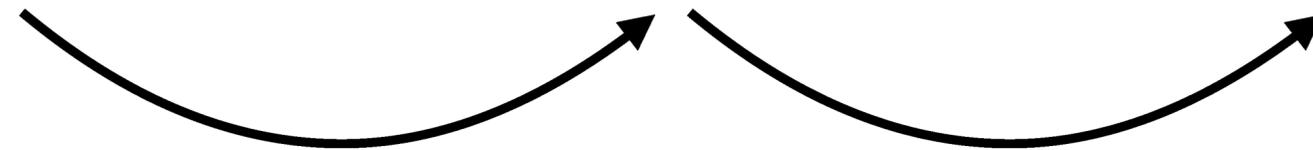
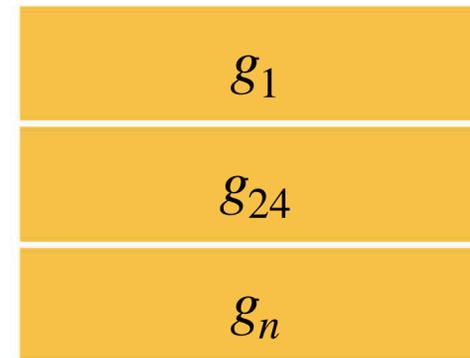
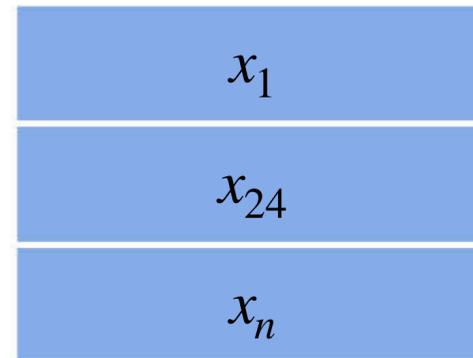
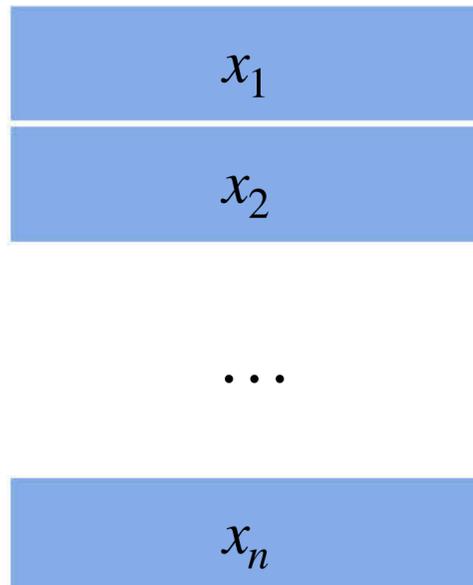
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1 iteration

Dataset

Batch

Gradients



**Sub-sampling** Gradient Computation

# DP-SGD

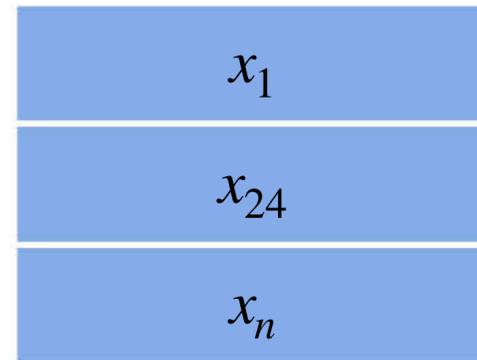
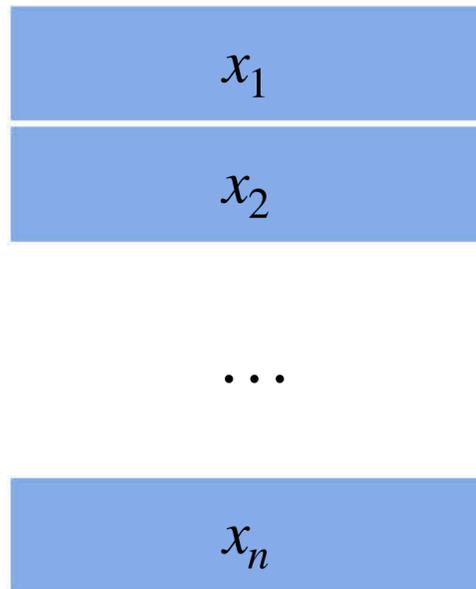
1 iteration

Dataset

Batch

Gradients

Clipped  
Gradients



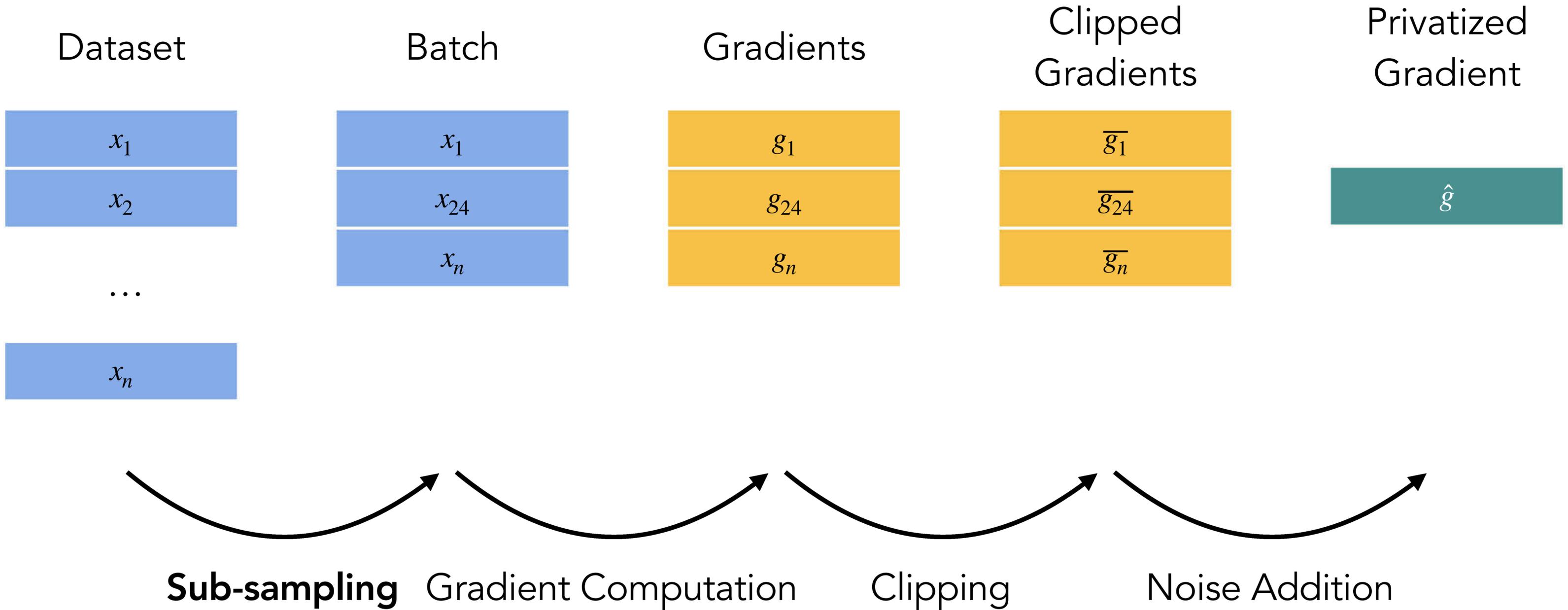
**Sub-sampling**

Gradient Computation

Clipping

# DP-SGD

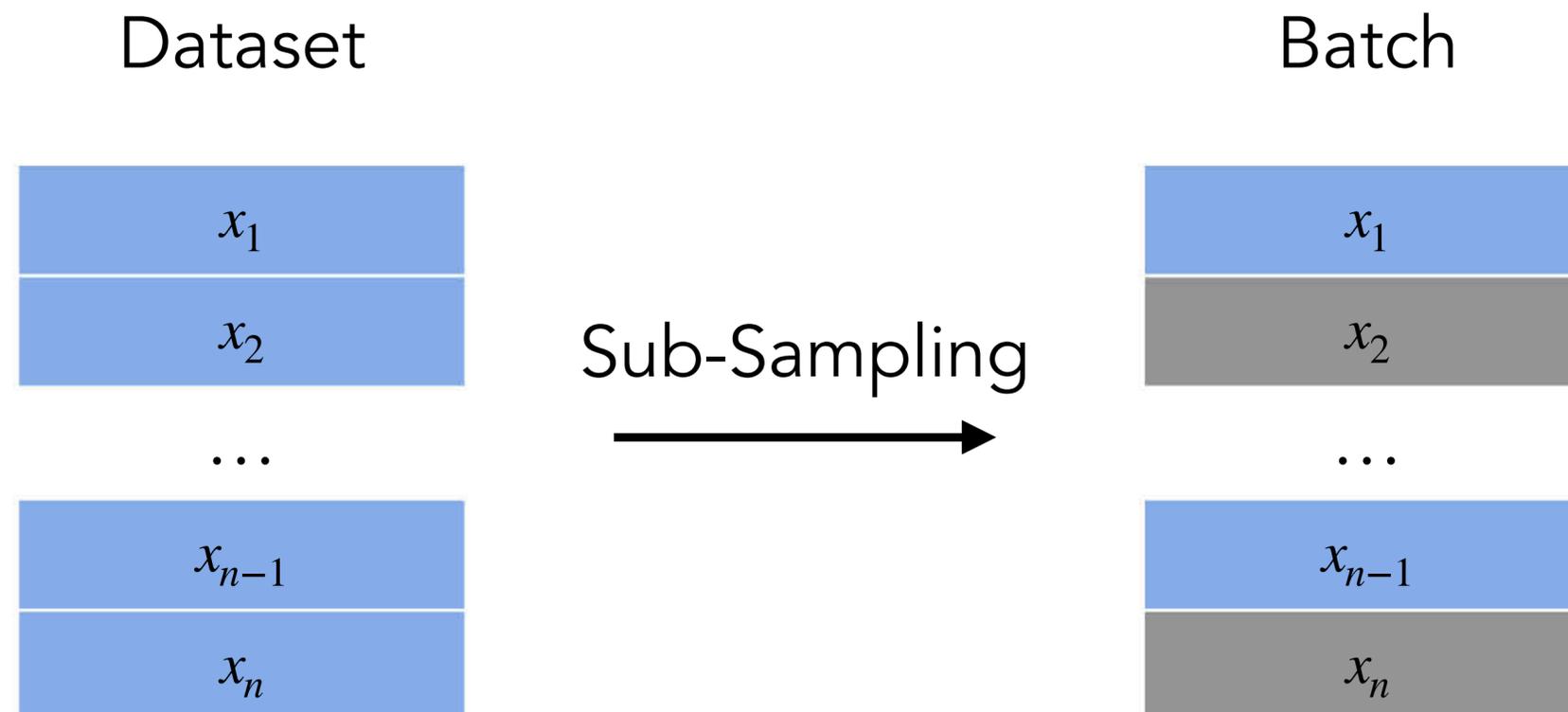
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# Sub-Sampling

## Why Sub-Sample?

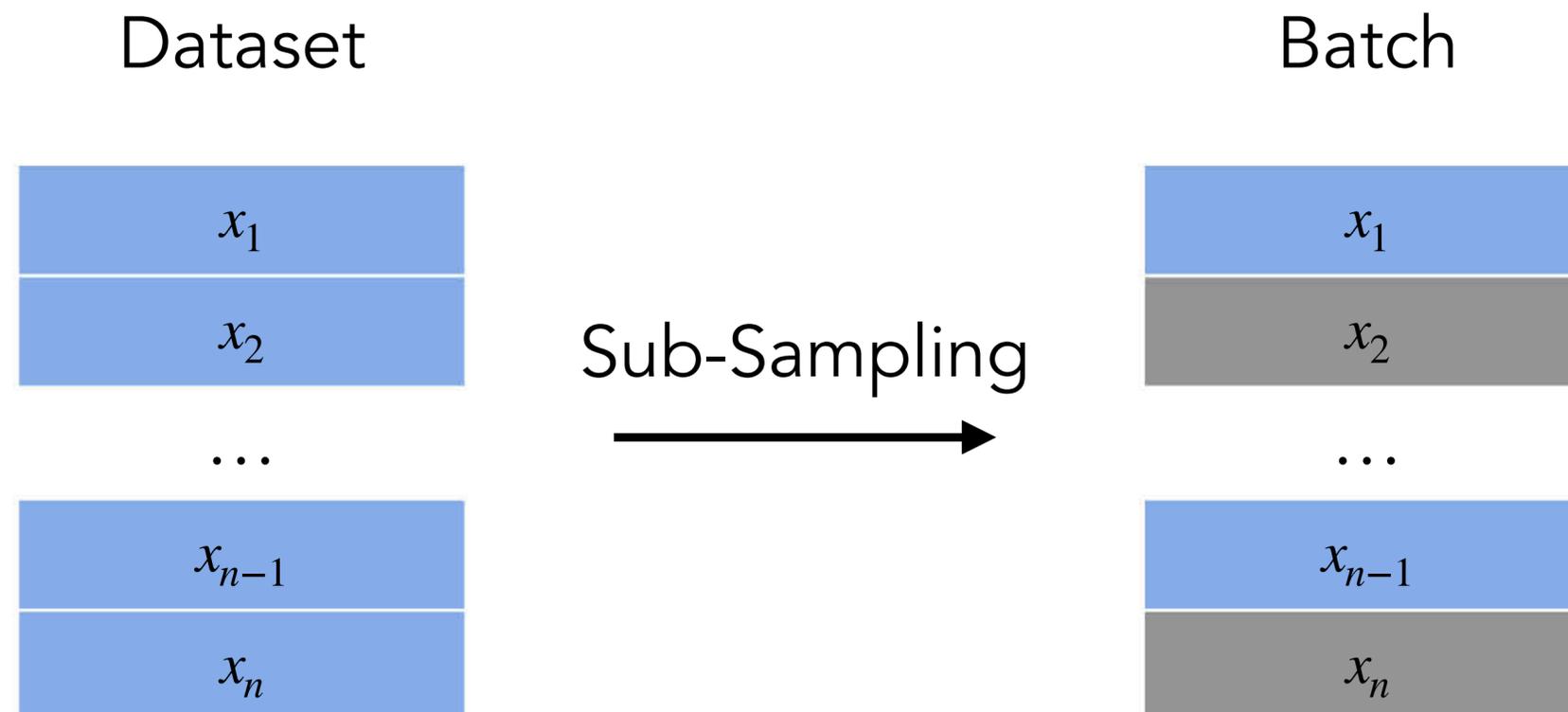
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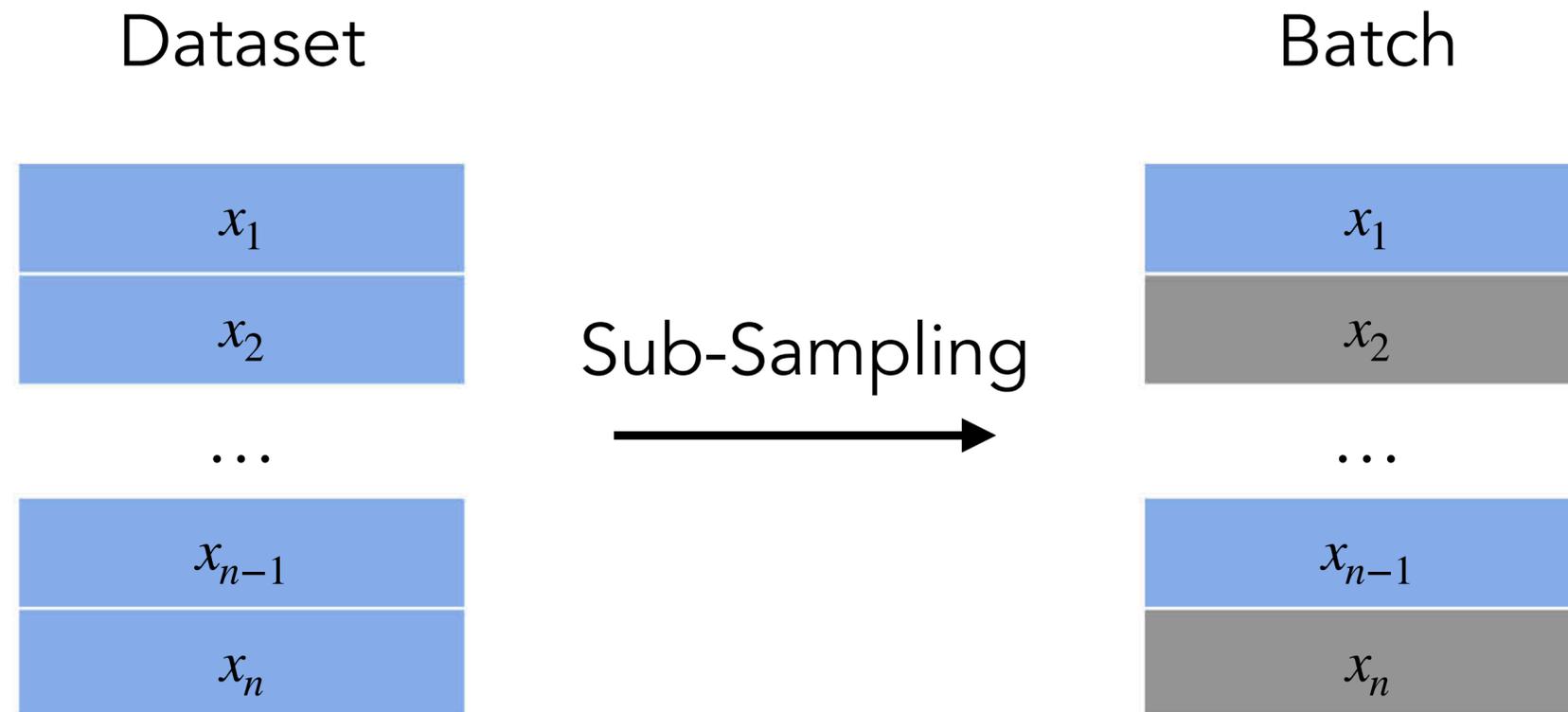
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- SGD naturally processes dataset in batches (for efficiency and utility)



# Sub-Sampling

## Why Sub-Sample?

- Sub-sampling: choosing batches through a random process
- SGD naturally processes dataset in batches (for efficiency and utility)
- Sub-sampling amplifies DP guarantees substantially<sup>1</sup>



<sup>1</sup> B. Balle, G. Barthe, M. Gaboardi. Privacy Amplification by Subsampling: Tight Analyses via Couplings and Divergences. NeurIPS, 2018.

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Speed	<b>Slow</b> , requires random access to entire dataset	<b>Fast</b> , iterate over $B$ records sequentially
Hardware Optimizations	<b>None</b> , due to random batch sizes	<b>XLA</b> optimization from fixed-batch size

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**Actual privacy guarantees of  
SOTA private models are unknown!**

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# DP Auditing

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Choose neighboring  
datasets

$D$



$D' = D + \text{Alice}$



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Run DP-SGD (Shuffle)  
repeatedly



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Inference Attack (MIA)



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Convert FPR and FNR  
to empirical  $\epsilon_{emp}$

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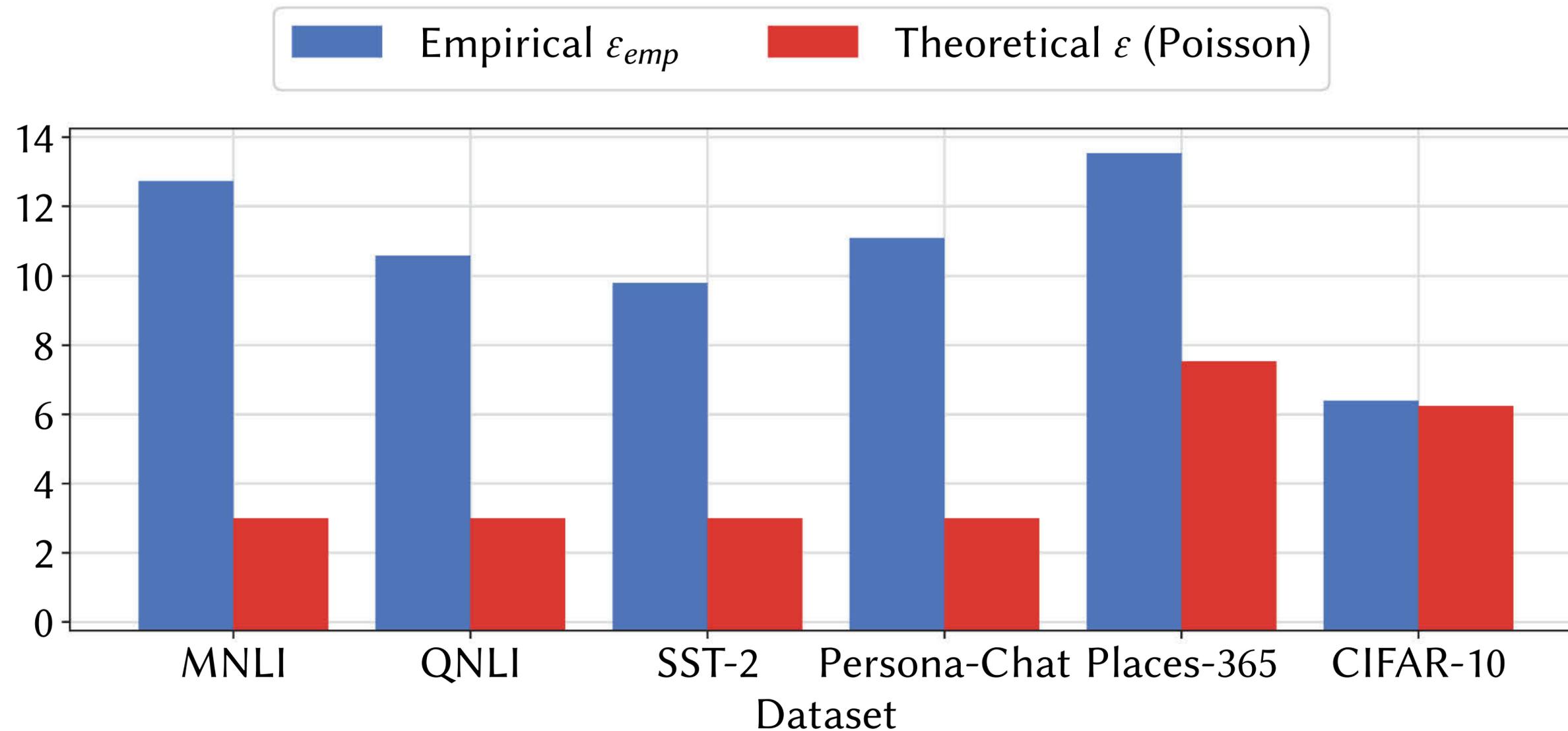
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# Experiments

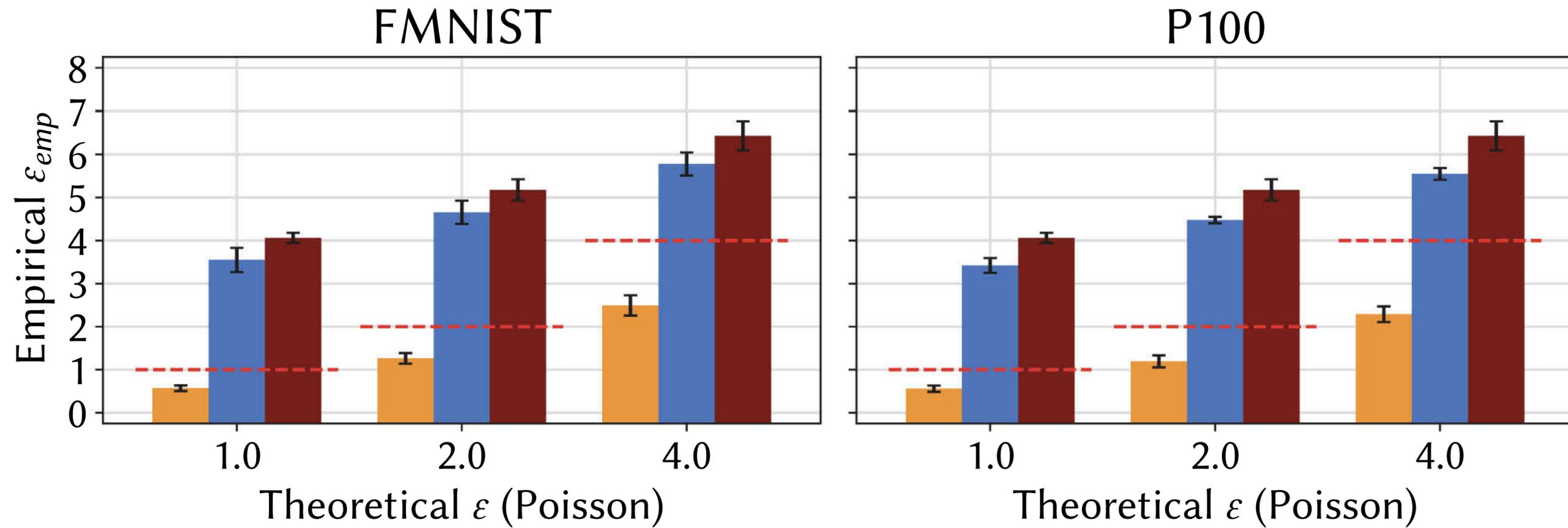
- **Datasets:** FMNIST, Purchase-100, CIFAR-10
- **Models:** LeNet, MLP, CNN
- Train 1M models for auditing

# SOTA models\* using Shuffling



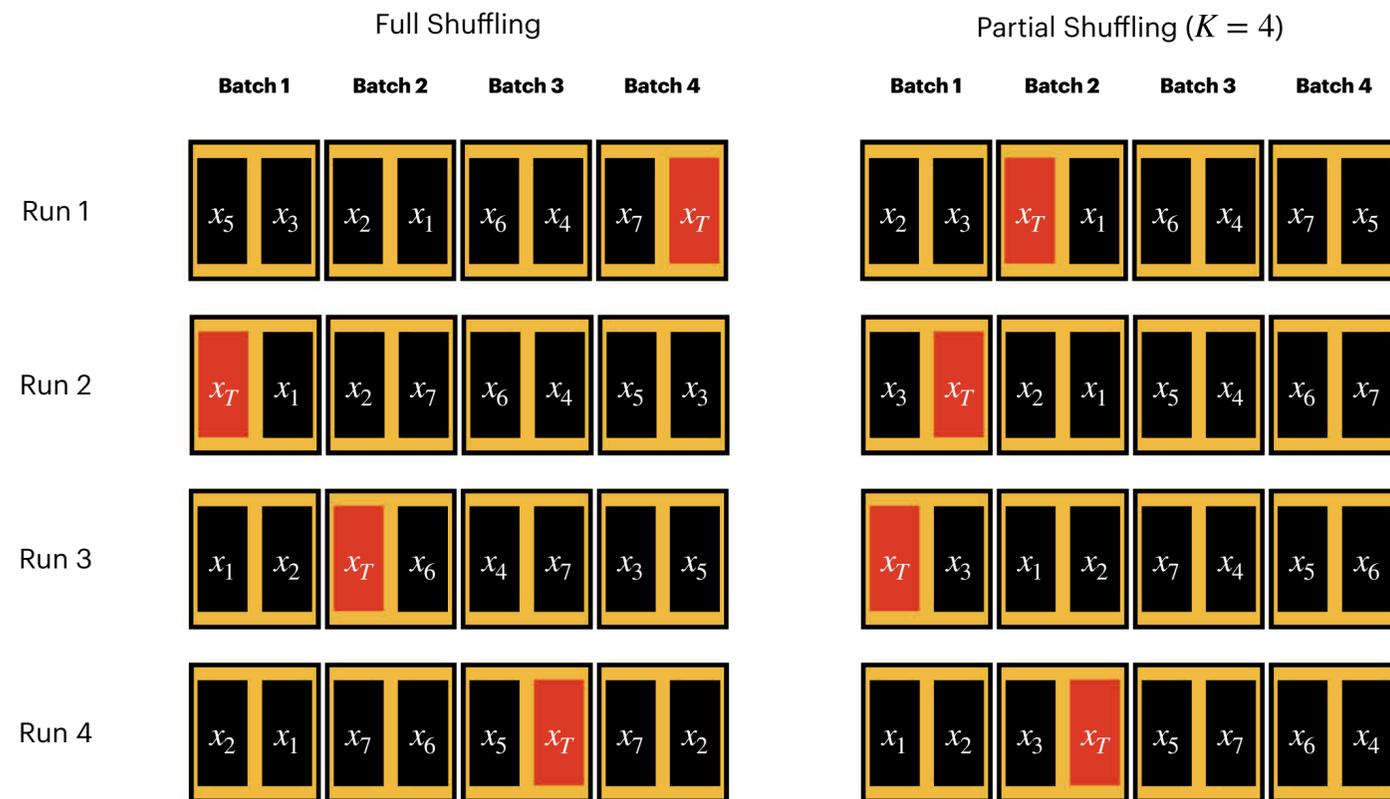
\*training on datasets is simulated under Worst-Case threat model

# Impact of Adversarial Power

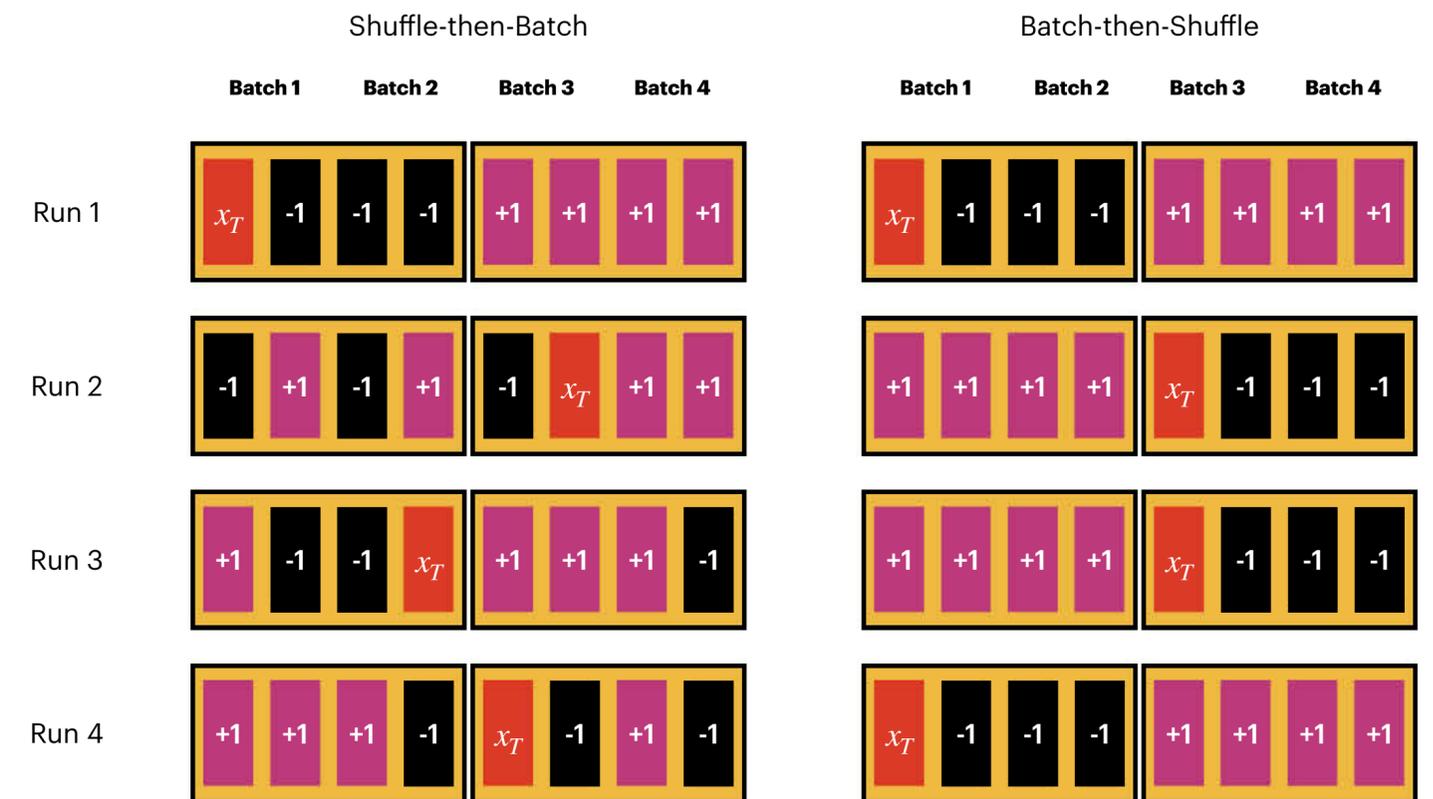


# Bugs in Shuffling

## Partial Shuffling

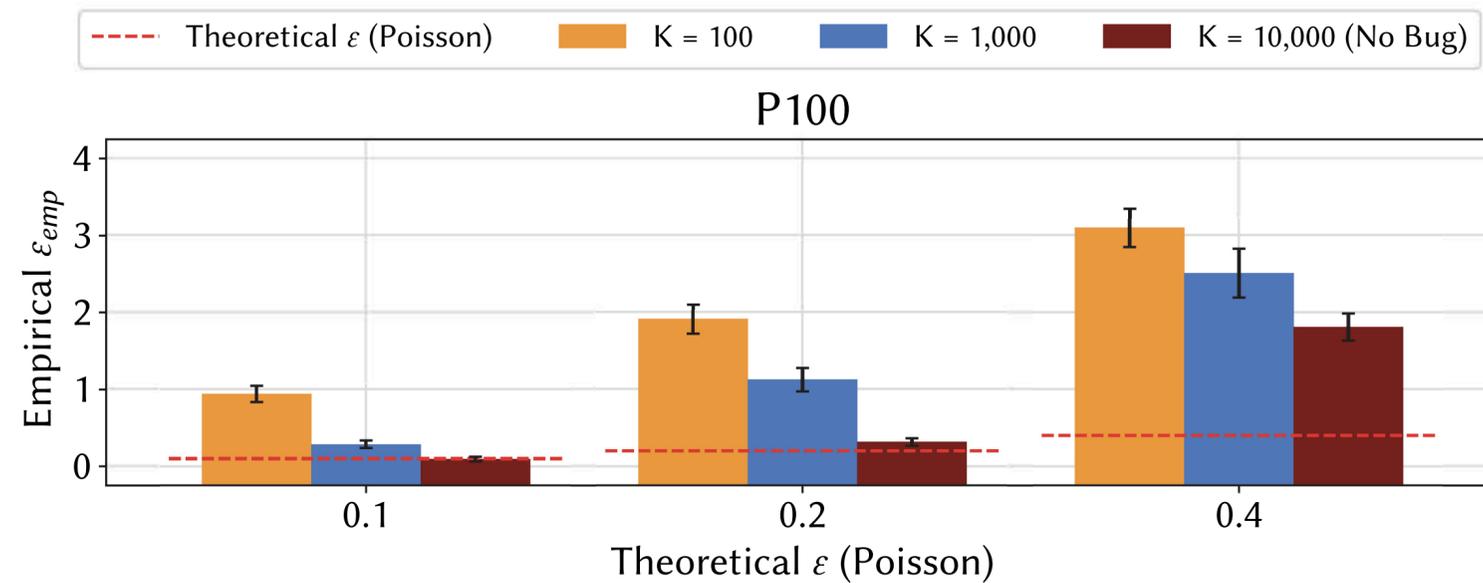


## Batch-then-Shuffle

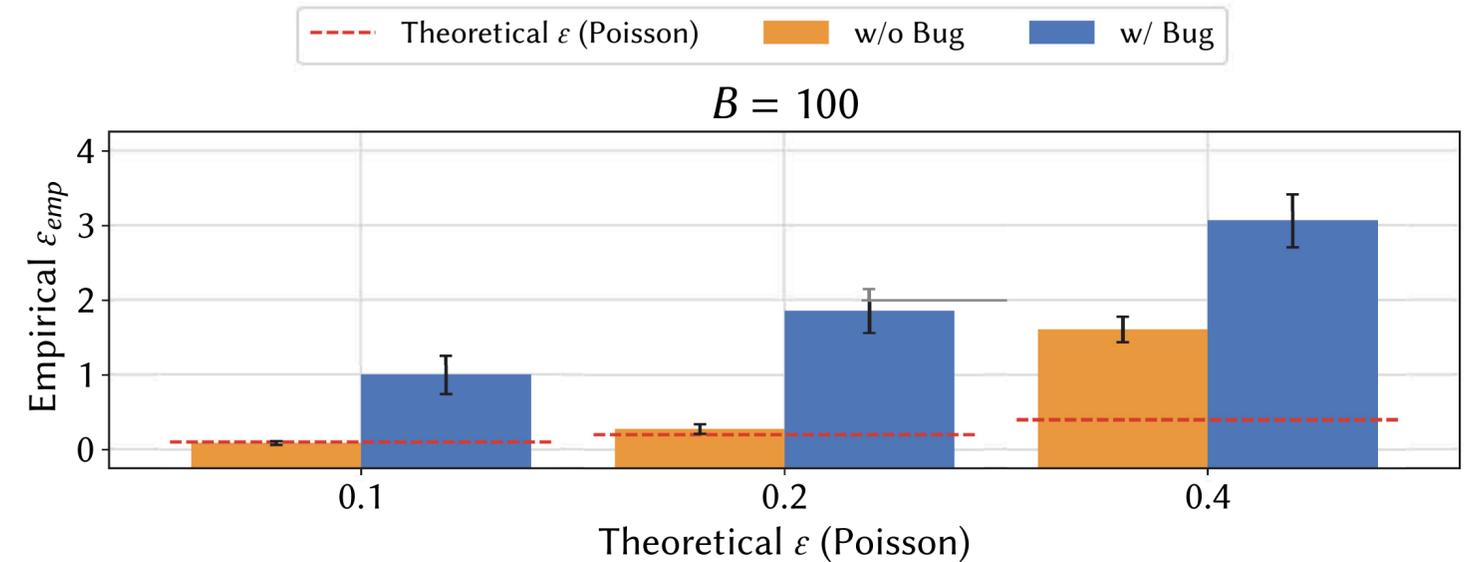


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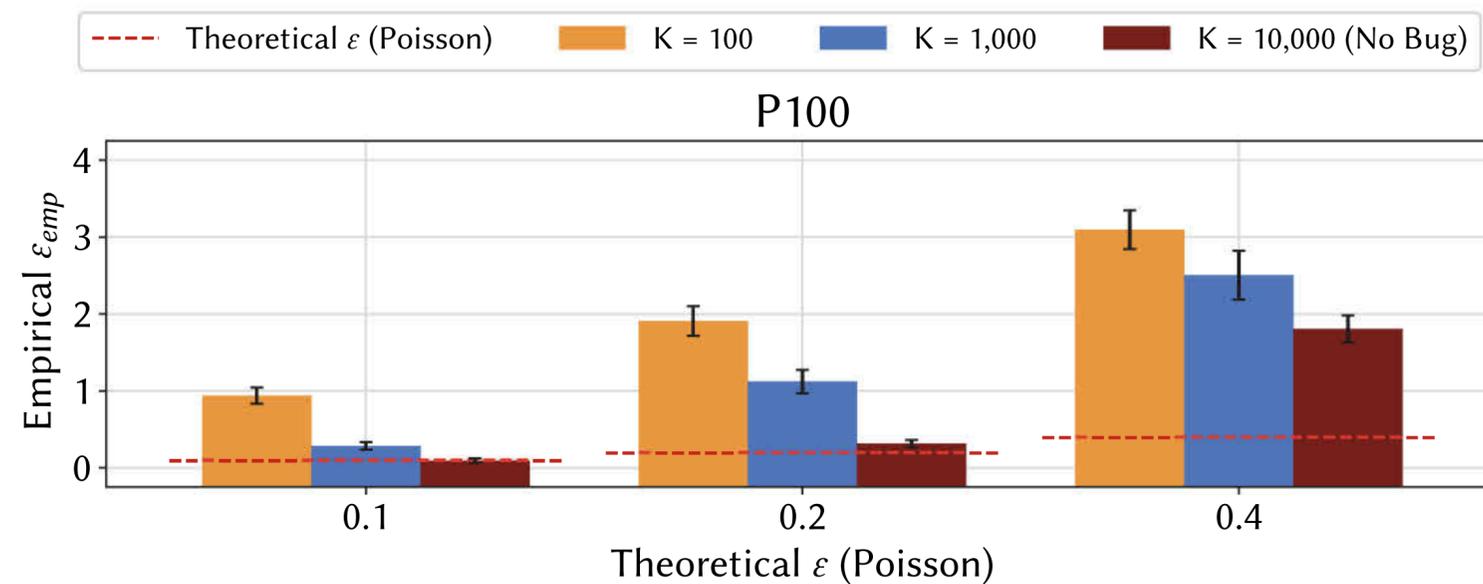


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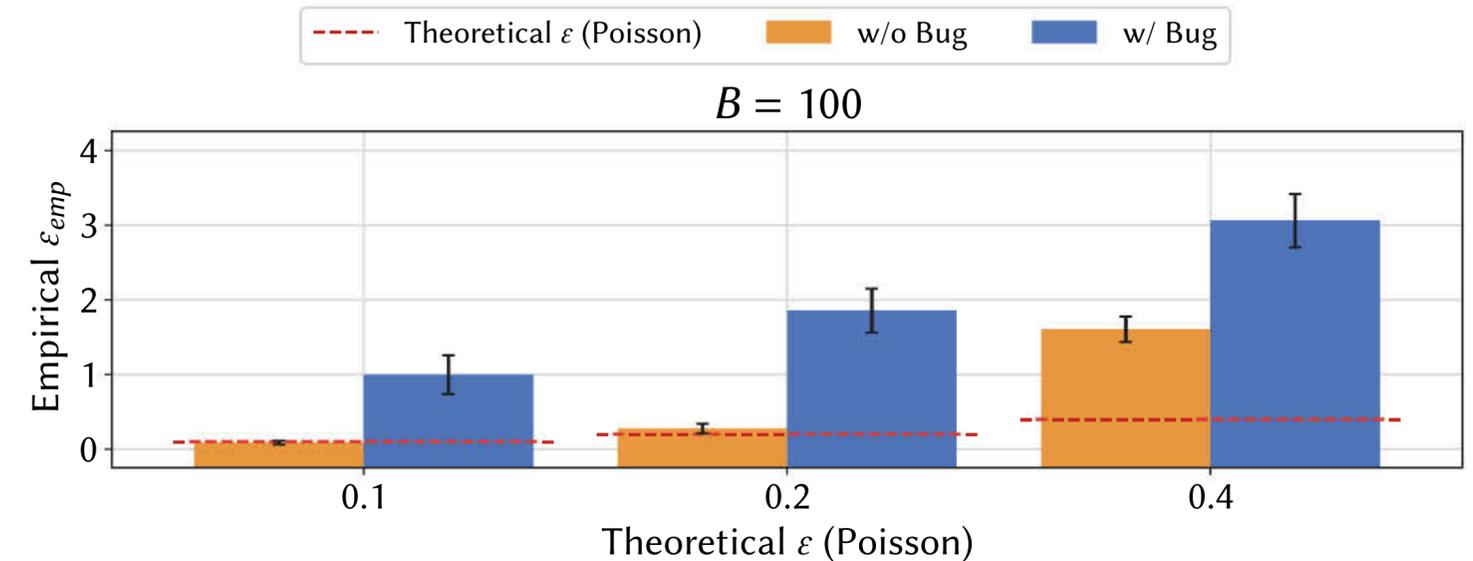


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**Bugs in shuffling can exacerbate gap between theoretical Poisson analysis and actual privacy leakage**

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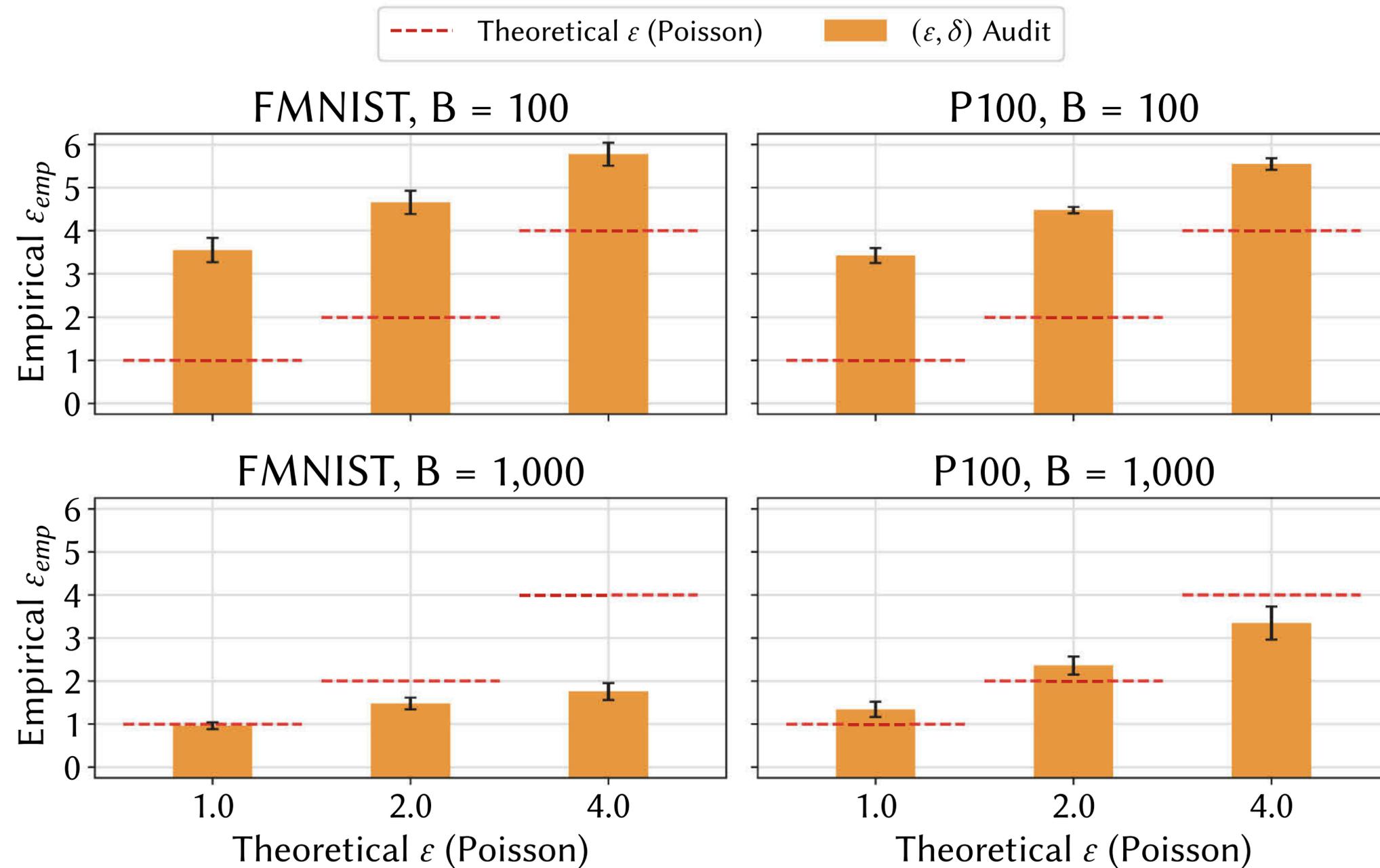


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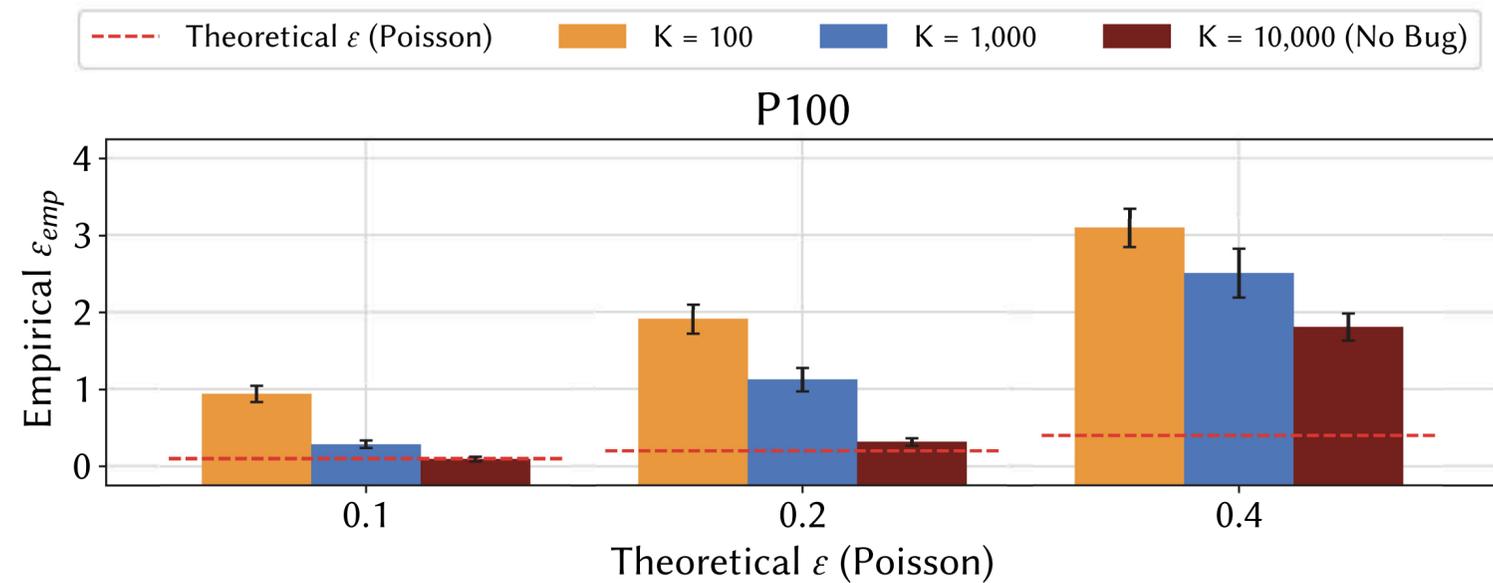


# Impact of Batch Size

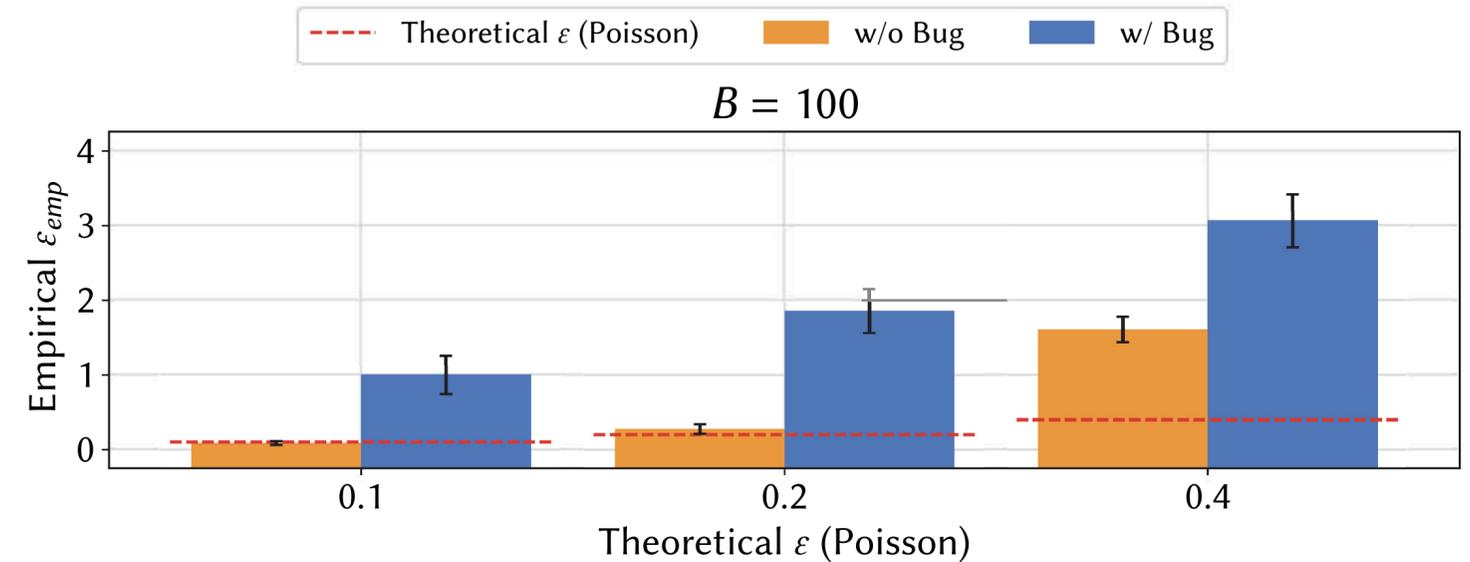


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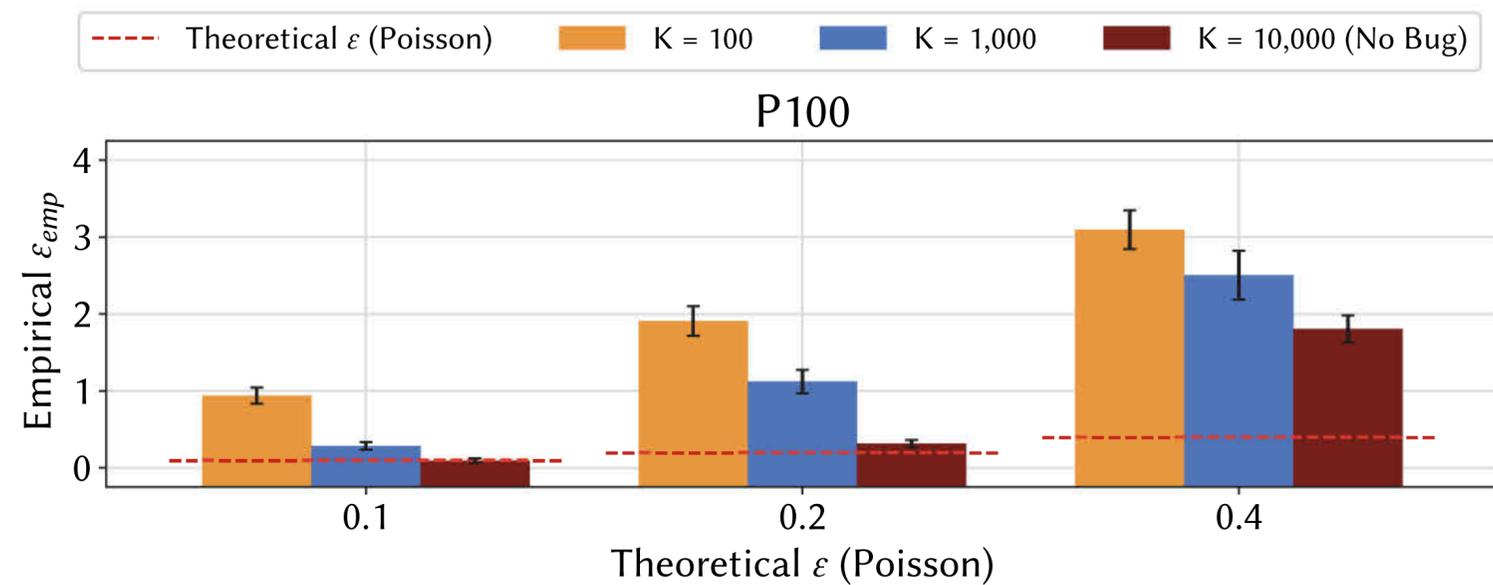


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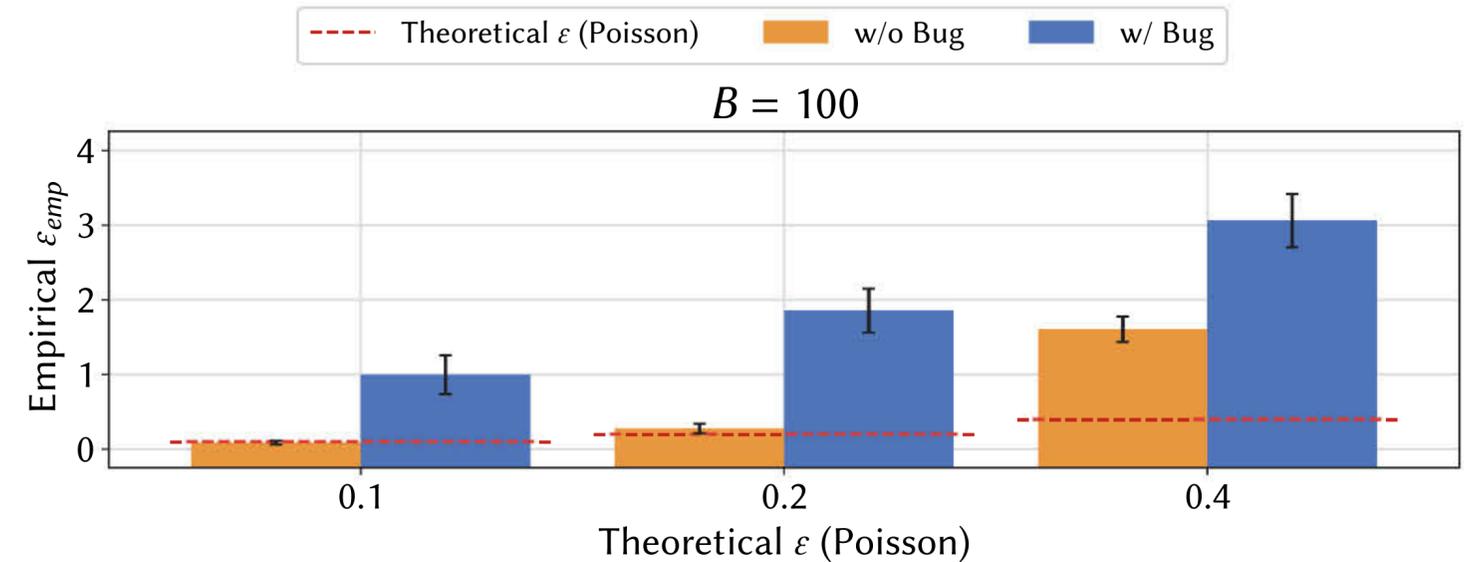


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